

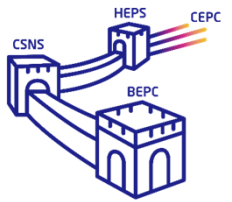
Design and experimental validation of high-resolution single-shot emittance diagnostics for heavy-ion beams

Ji-Gwang Hwang, Gangneung-Wonju Nat'l Univ. (GWNU)

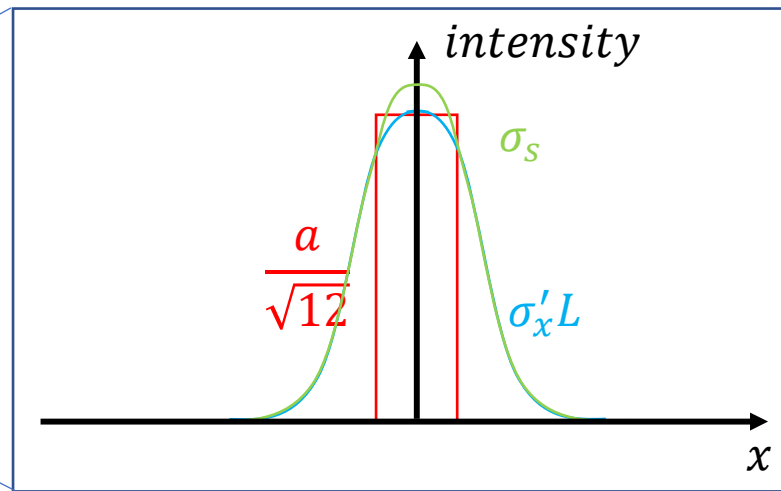
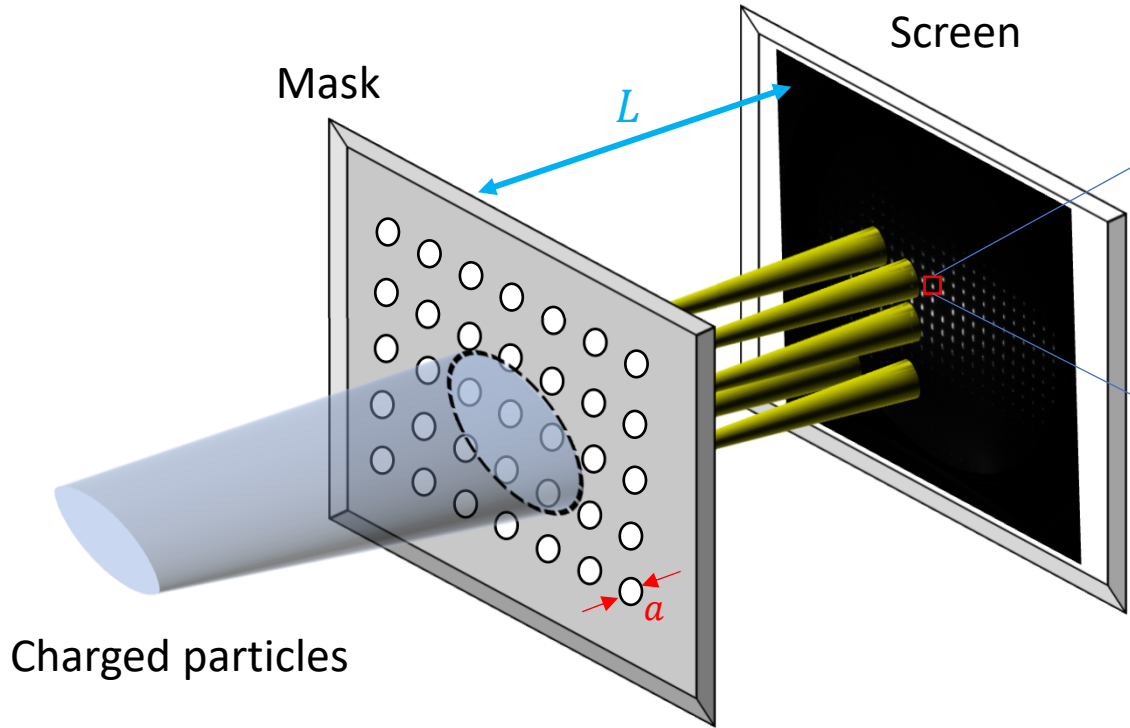
Garam Hahn, Pohang Accelerator Laboratory (PAL), Rep. of Korea



Principle of Pepper-pot device



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The rms spot size on the screen σ_s is given by

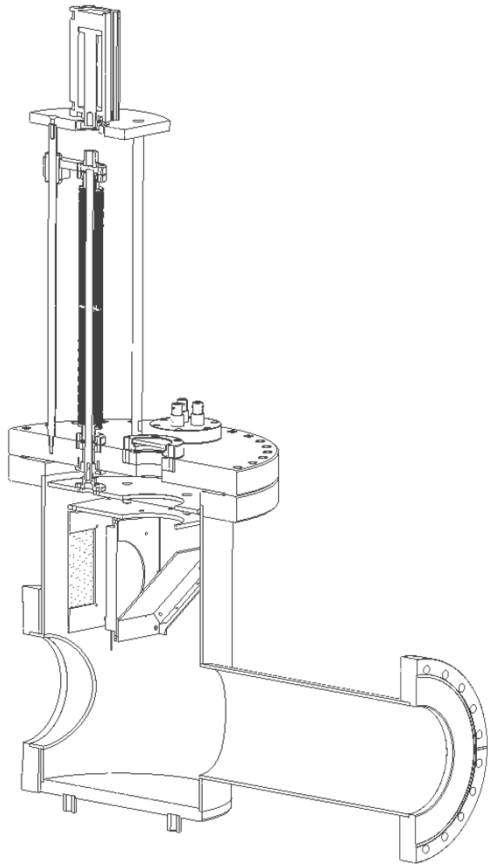
$$\sigma_s = \sqrt{\left(\frac{a}{\sqrt{12}}\right)^2 + (\sqrt{\varepsilon\gamma}L)^2},$$

where ε denotes the emittance and γ is the Twiss parameter. The factor $1/\sqrt{12}$ comes from considering the rms of the flattop distribution created by the slit projection.

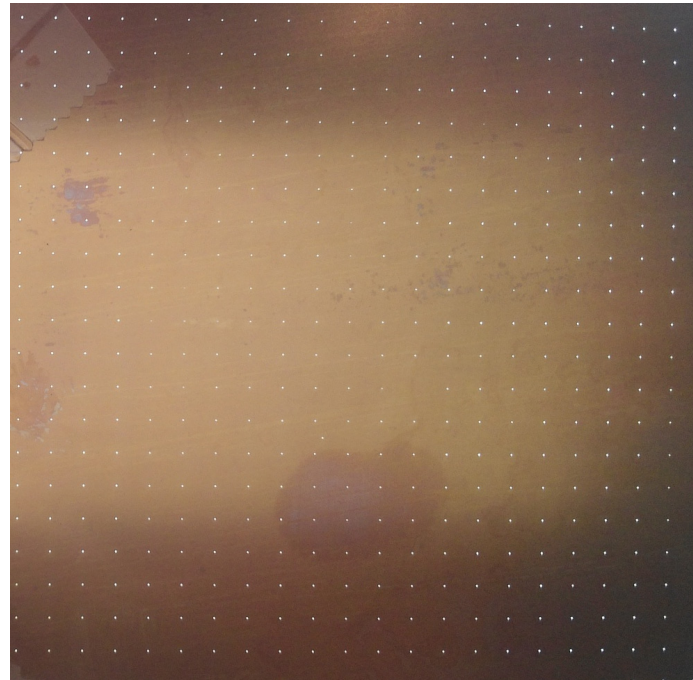
High resolution \rightarrow Small hole \rightarrow Low intensity
 \downarrow
 Limited resolution \leftarrow Noise \leftarrow Micro-Channel Plate



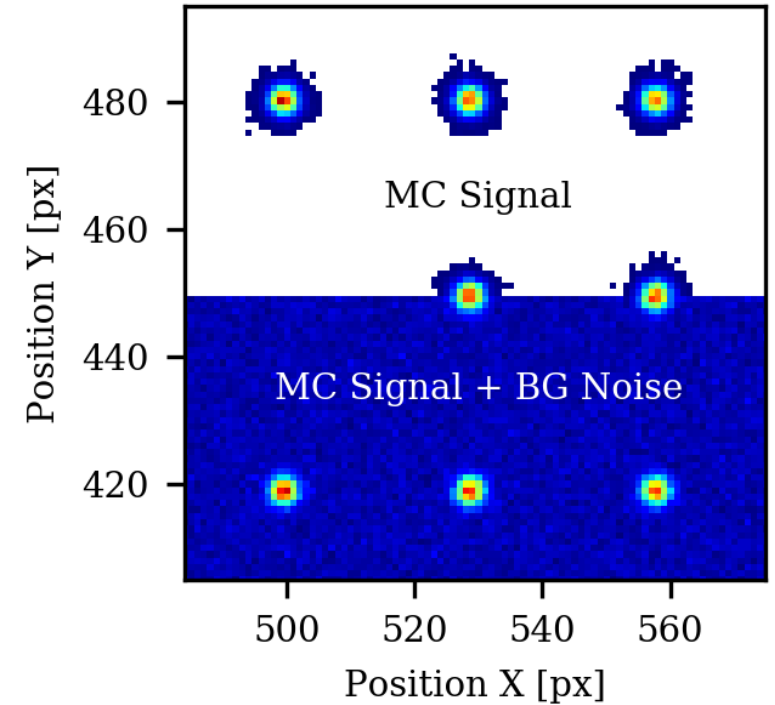
Design considerations and issues



Design recipe
(hole size, distance,...)



Mask manufacturing
(Laser, Etching,...)



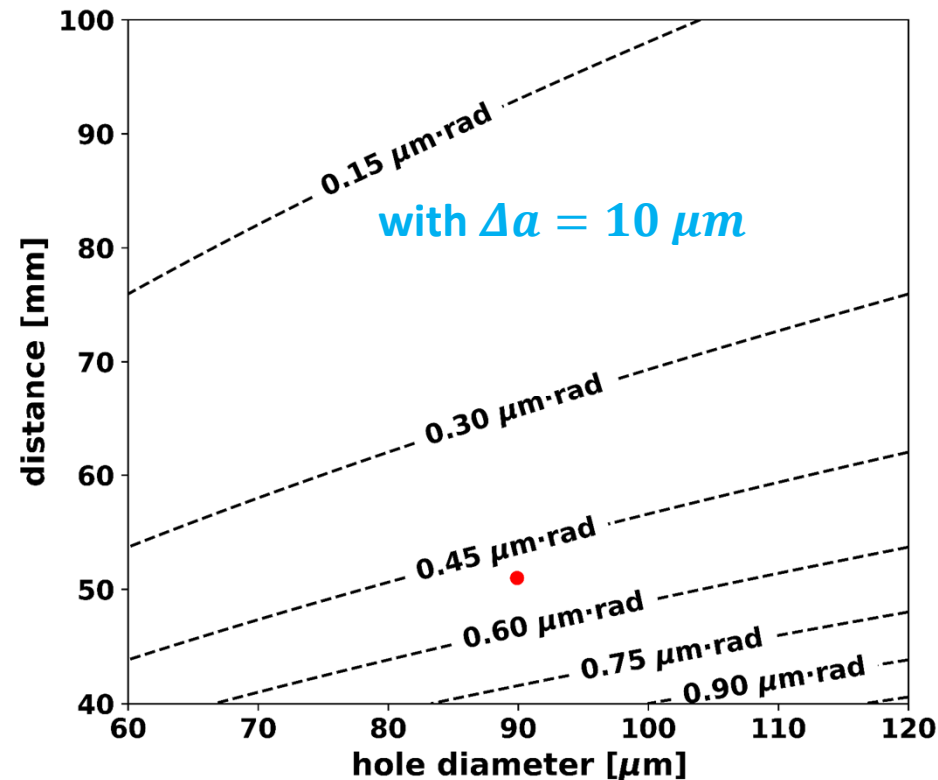
Noise subtraction
(Floor cut, + extrapolation
sophisticated filters, ...)

Design considerations

- Resolution calculation with hole size inaccuracy

$$\Delta\varepsilon = \frac{2\Delta a}{\gamma L^2} \left(2\sigma_s \frac{\partial\sigma_s}{\partial a} - \frac{2a}{\sqrt{12}} \right)$$

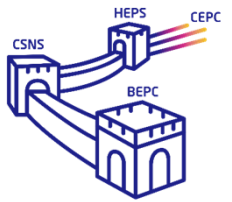
- hole size inaccuracy Δa (?)
 - hole diameter a (60~150 μm)
 - MCP-to-mask distance L (40~150 mm)
 - γ are the Twiss parameters
- For our beamline, the installation space is limited (less than 10 cm total)
 - LEBT emittance: ~ 30 nm-rad



MAIN SPECIFICATIONS OF THE DESIGNED PEPPER-POT DEVICE

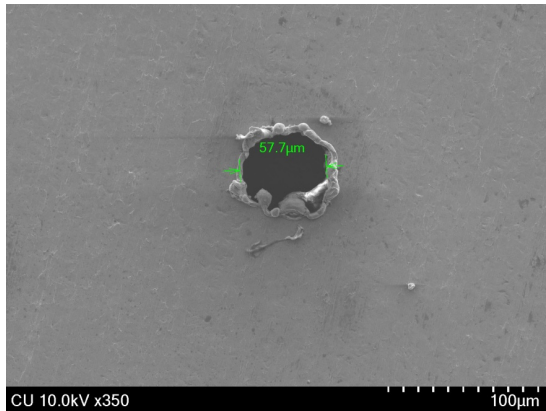
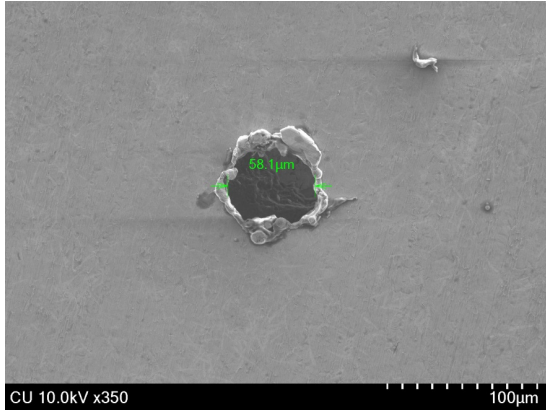
| Name | Value | Unit |
|------------------------------|------------|---------|
| Dimension of mask hole-array | 75 × 75 | mm |
| Mask hole configuration | 25 × 25-1 | – |
| Mask hole-to-hole distance | 3.0 | mm |
| Mask hole diameter | 89.9 ± 1.3 | μm |
| Mask to MCP distance | 51 | mm |
| MCP active radius | 37.5 | mm |

Mask production



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Laser-cutting



Small and irregular holes

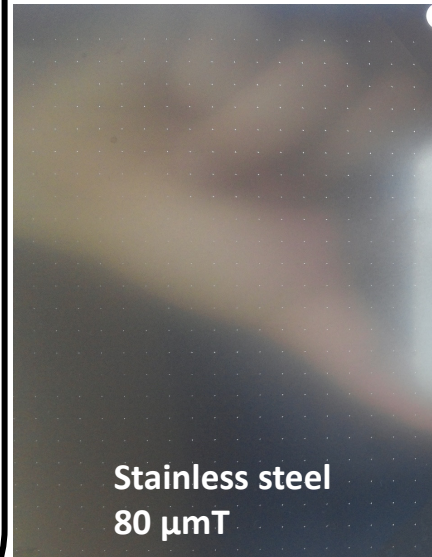
Requirements

Diameter: less than $90\mu\text{m}$

Mask size: $8.5\text{ cm} \times 8.5\text{ cm}$

of holes: $25 \times 25 - 1$ (*at center)

Laser-cutting



Stainless steel
 $80\ \mu\text{mT}$

$\langle a \rangle = 58\mu\text{m}$

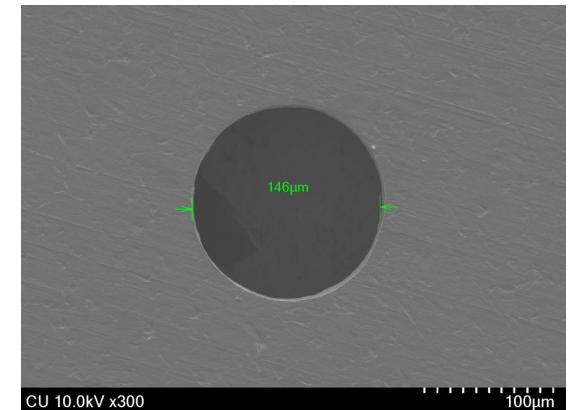
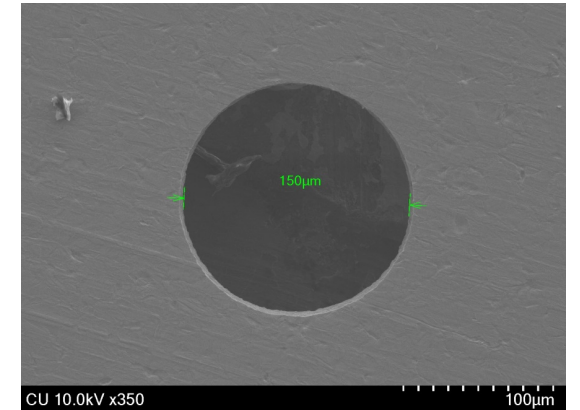
Photolithography



Phosphor bronze
 $50\ \mu\text{mT}$

$\langle a \rangle = 150\mu\text{m}$

Lithography



Large diameter but clean

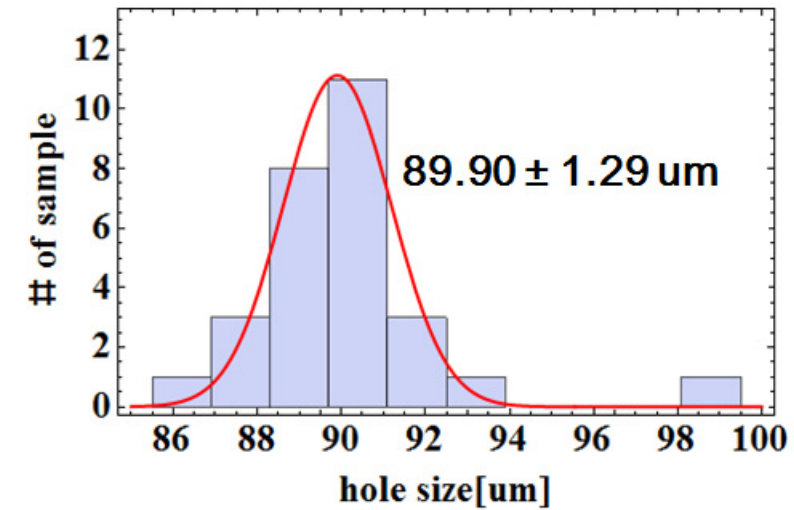
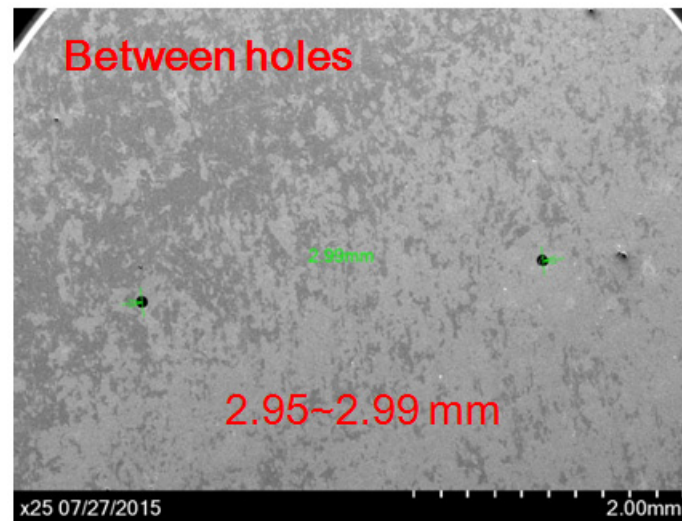
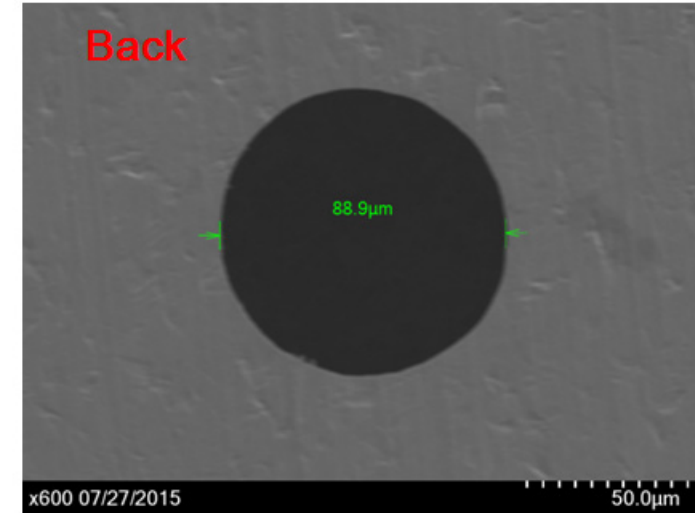
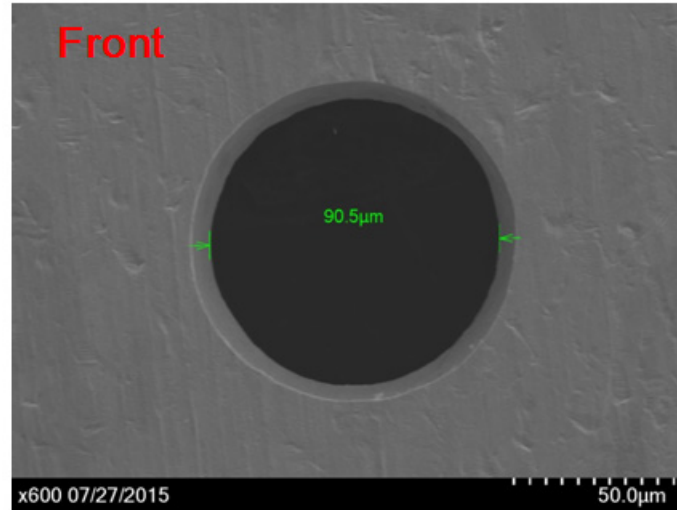
Controllable by
Manufacturing procedure



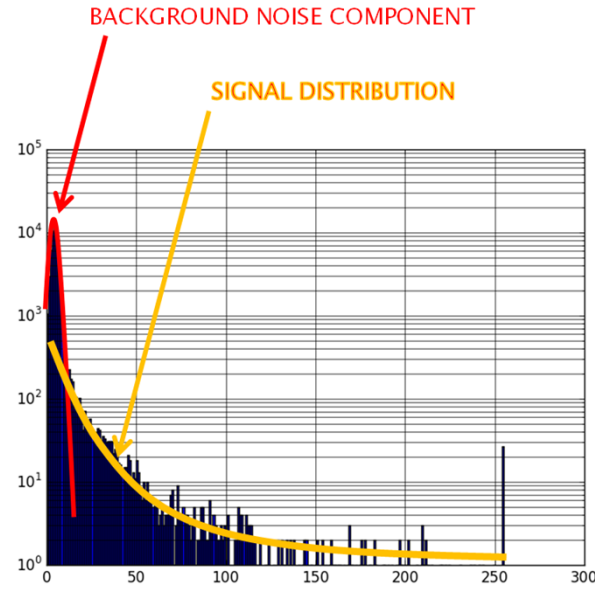
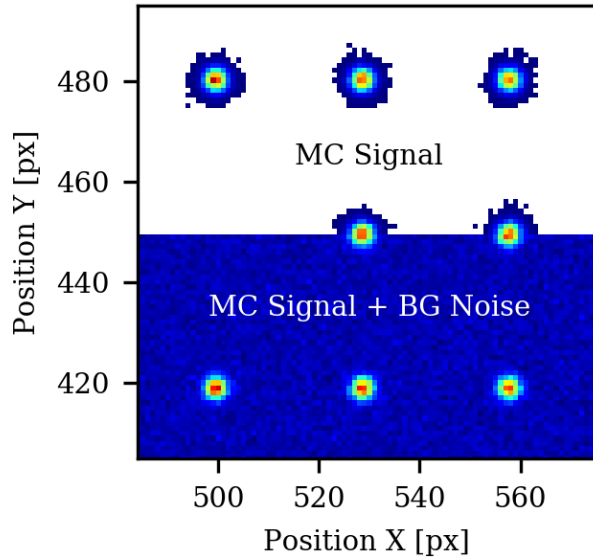
Mask production



Scanning Electron Microscope
- 5 cm x 5 cm sample



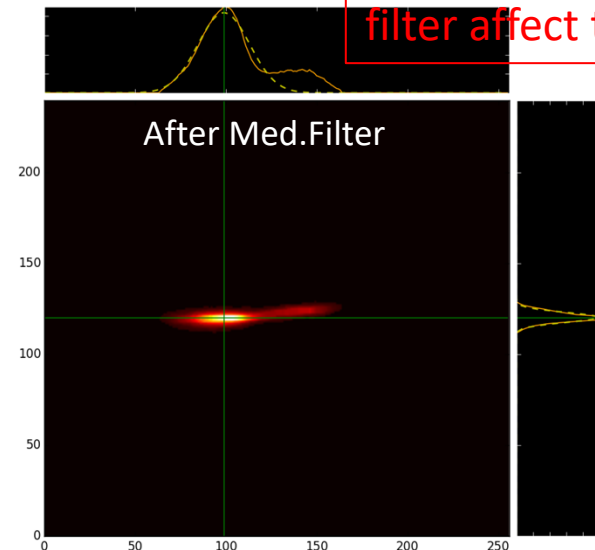
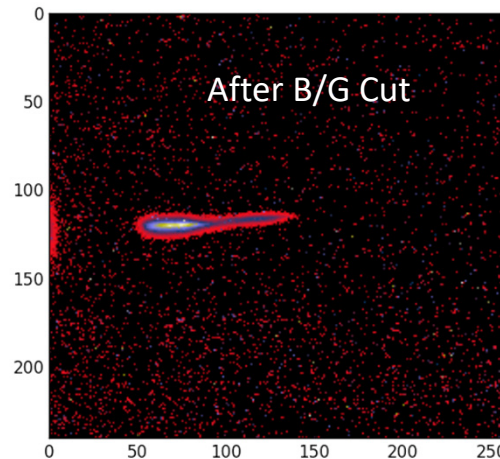
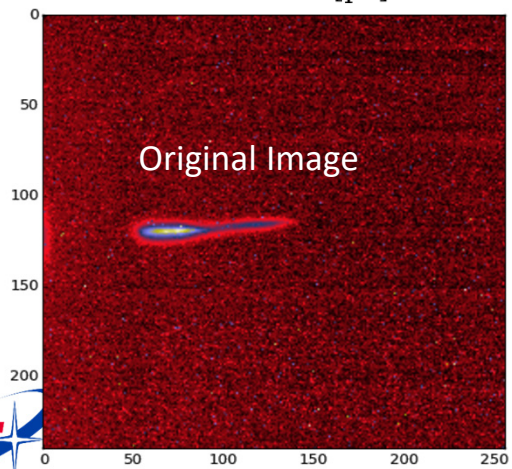
Background + noise subtraction



ALGORITHM WORK-FLOW

For the spectrum analysis

1. find the lowest peak
2. Pick a sample point for fitting around hilltop
3. make a curve fit
→ get std. deviation
4. subtract the threshold ($\sim 2.5\sigma$)
5. Apply median filter (with a kernel of 5 pixels)



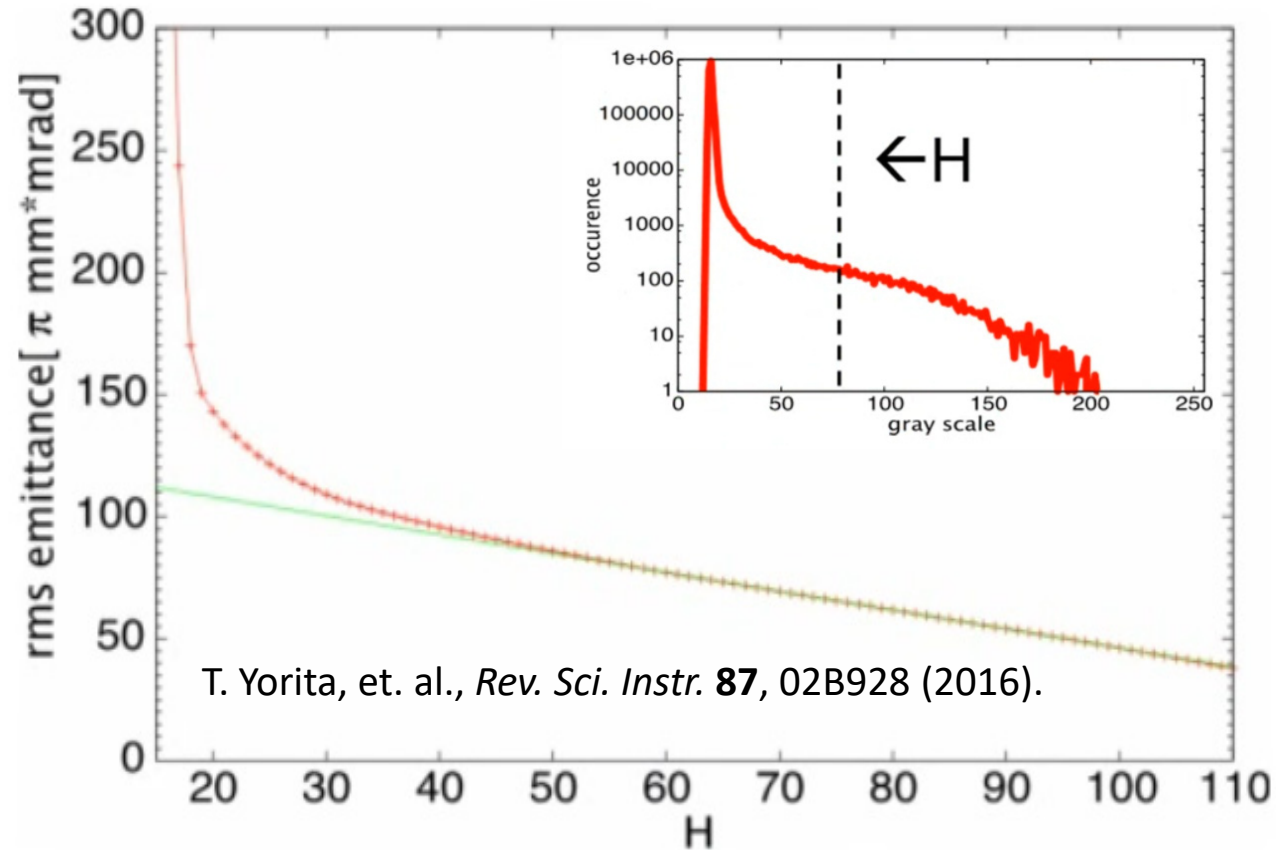
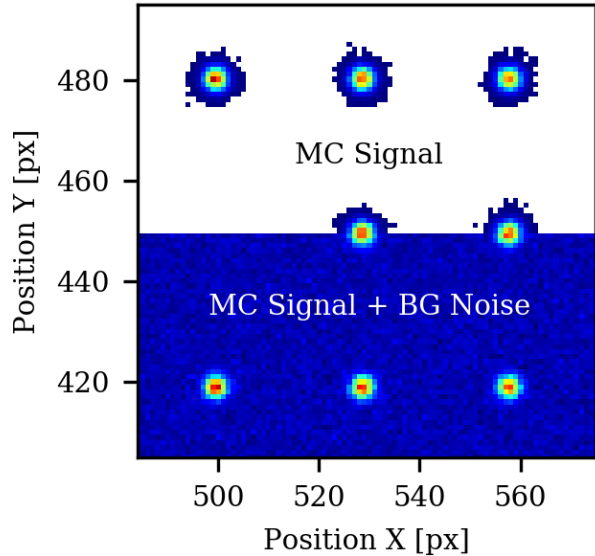
BG noise cut and median filter affect the real signal

Background + noise subtraction

BACKGROUND NOISE COMPONENT

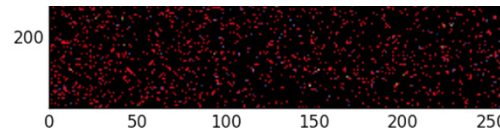
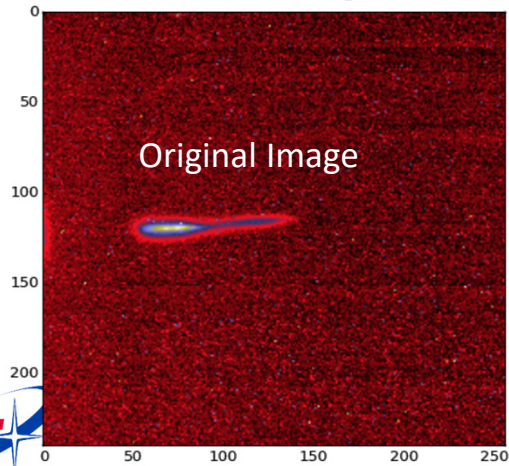
SIGNAL DISTRIBUTION

ALGORITHM WORK-FLOW



i)
rnel of 5 pixels)

noise cut and median
r affect the real signal



Algorithm test with virtual image

- MC-GEN – MonteCarlo event generator
Gaussian Twiss beam Gen.
* Misalignment error + Dist. error
- SIM-DIGI – Transform and Digitization
Convert to a bitmap image
* MCP and CCD resolution-related error

intensity level of each pixel

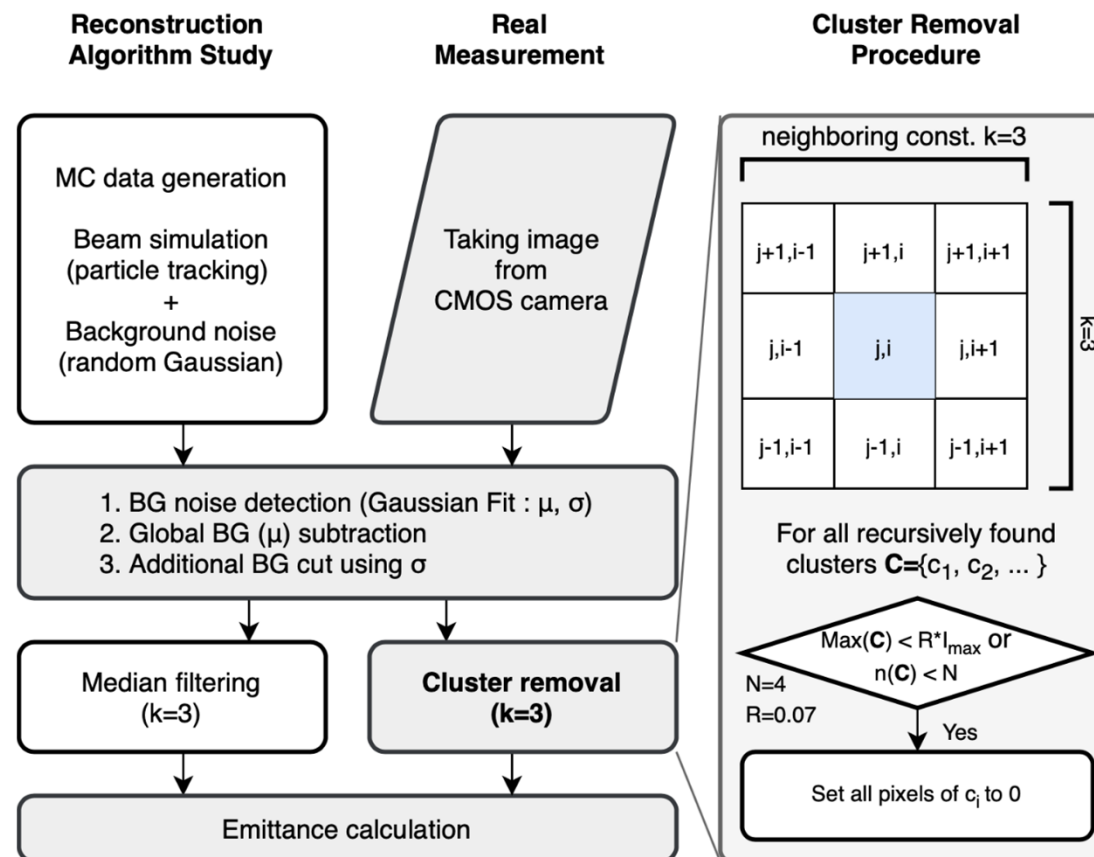
$$n(\vec{X}_{i,j}) = \left[A e^{-\frac{(x-x_i)^2}{2\epsilon_x\beta_x}} e^{-\frac{(y-y_j)^2}{2\epsilon_y\beta_y}} \right]$$

Gaussian beam distribution model
applying Twiss parameters

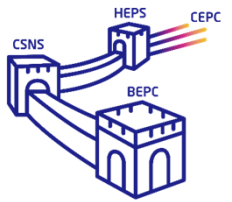
$$x'_i, y'_j = G_r \left(-\frac{\alpha_x}{\beta_x} x_i, \sqrt{\frac{\epsilon_x}{\beta_x}} \right), G_r \left(-\frac{\alpha_y}{\beta_y} y_j, \sqrt{\frac{\epsilon_y}{\beta_y}} \right),$$

- RECO – Reconstruction toolkit

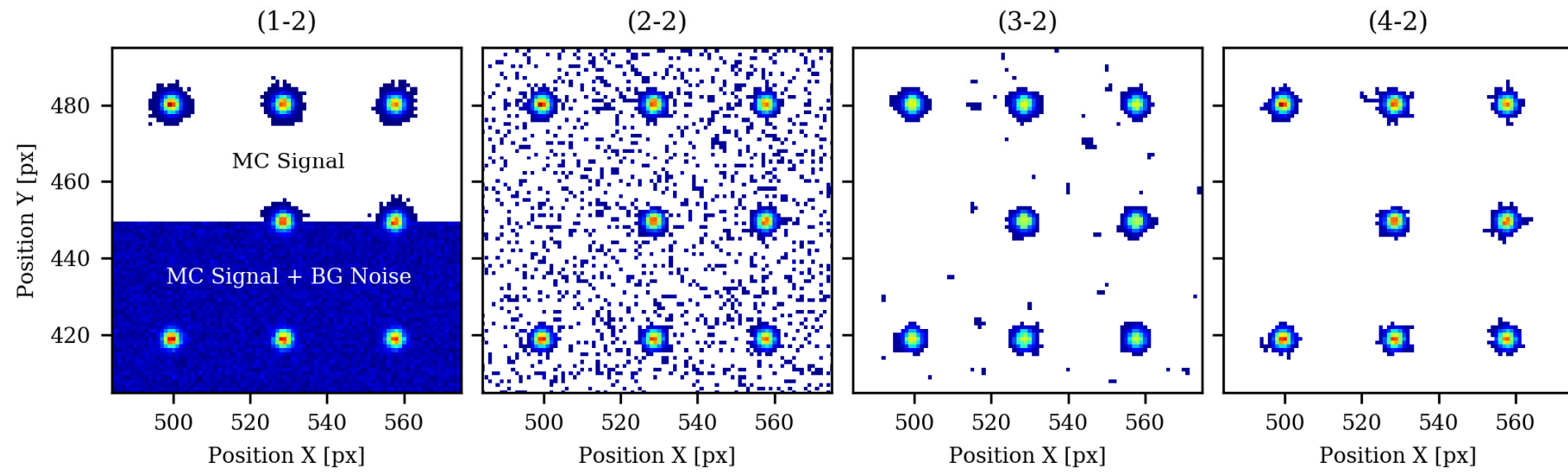
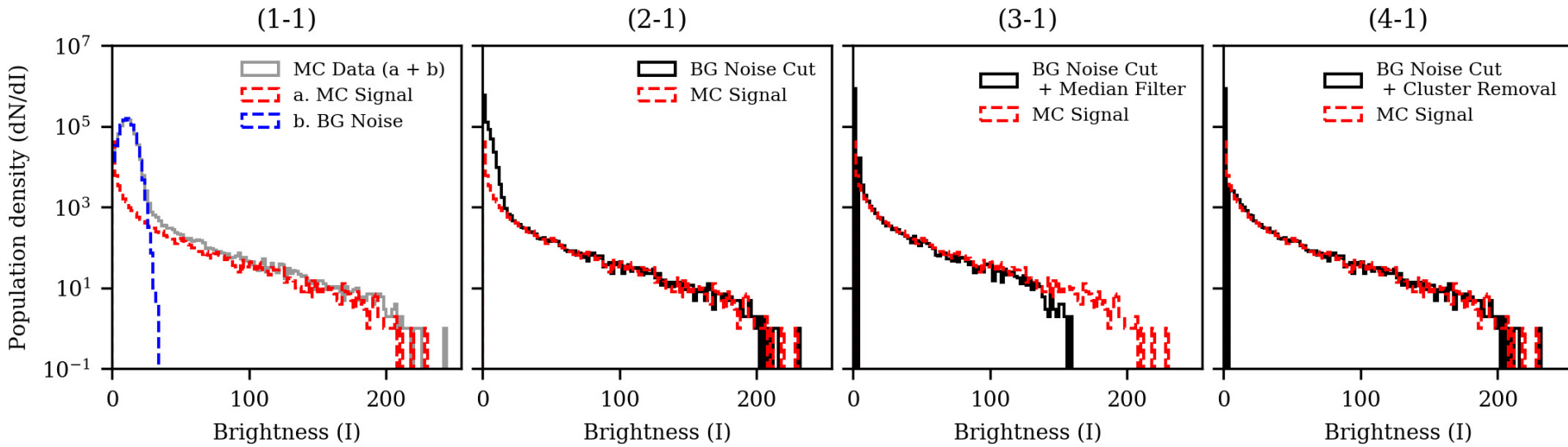
- Mc level : comparing RECO to MC, Def. error bars
- RECO level : making production GUI console



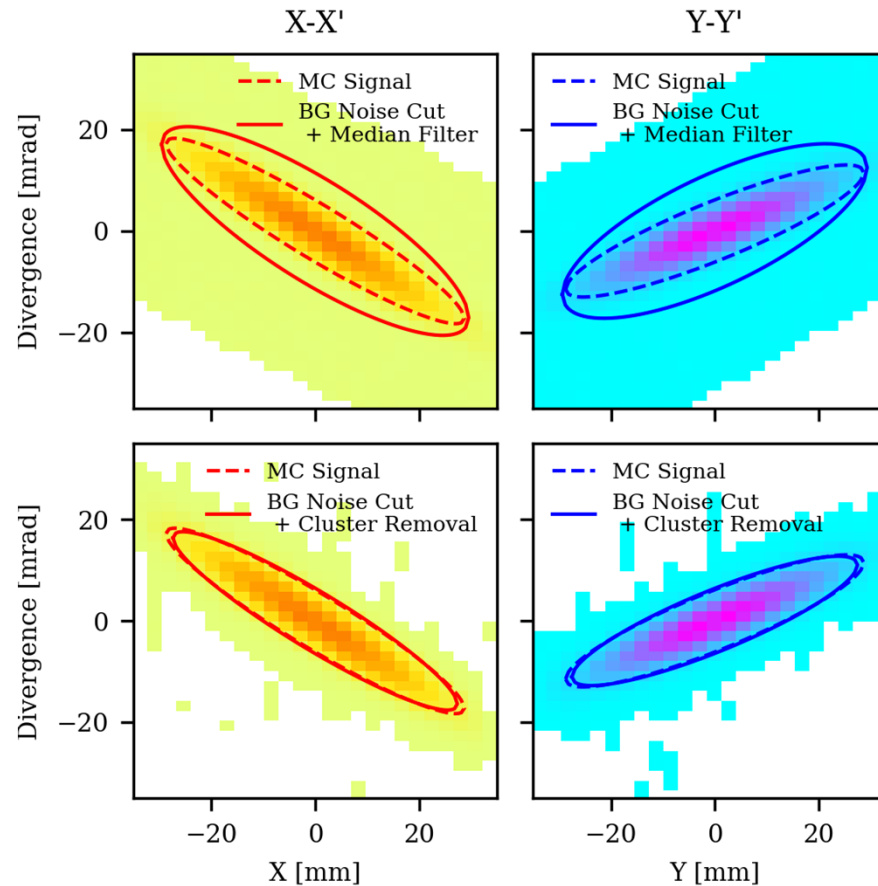
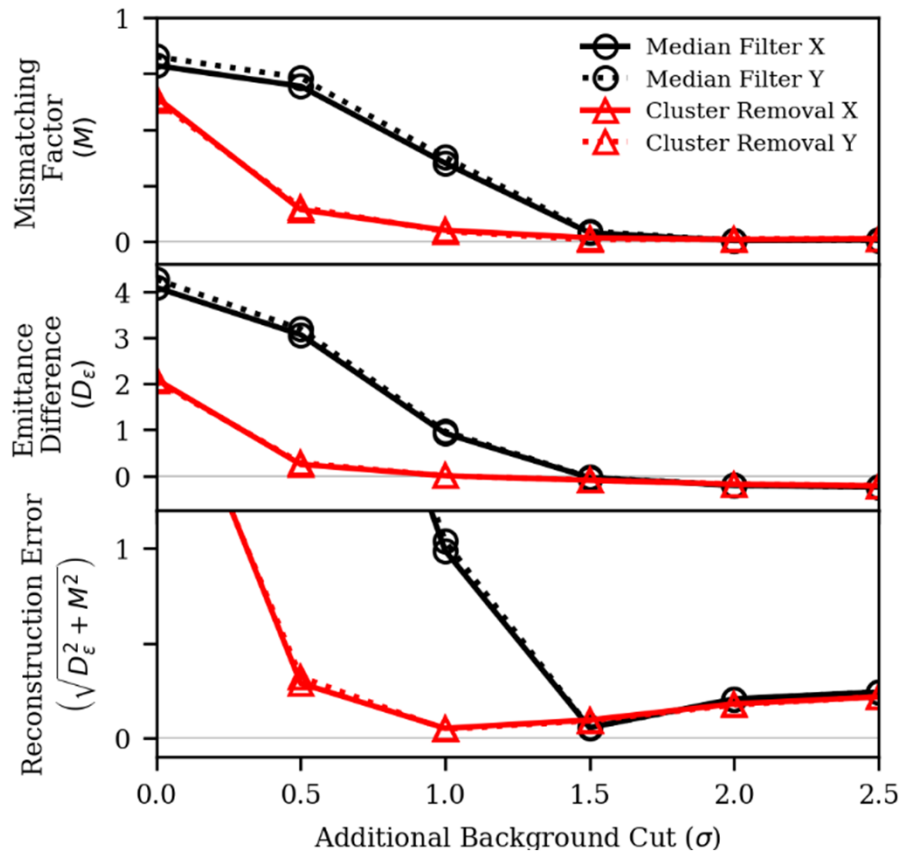
Cluster removal algorithm



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Cluster removal algorithm

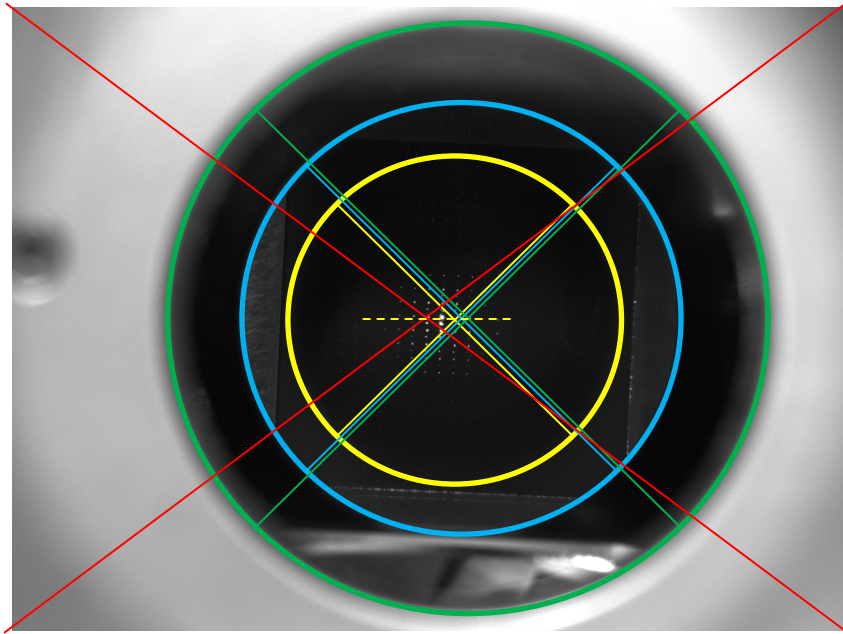


The additional background cut (1.0σ) is necessary and the level was investigated to minimize the

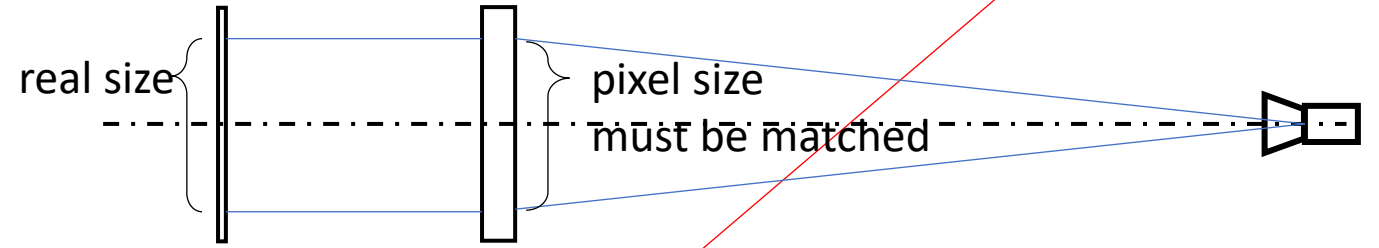
mismatching factor ($M = \sqrt{(R + \sqrt{R^2 - 4}/2 - 1)}$) and emittance misreading $D_\epsilon = (\epsilon_r - \epsilon_m)/\epsilon_m$.

$$R = \beta_r \gamma_m + \beta_m \gamma_r - 2\alpha_m \alpha_r \quad \text{G. Hahn, J.-G Hwang, et. al., } IEEE \text{ Tras. Instr. and Mea. } \mathbf{70}, 5015507 \text{ (2021).}$$

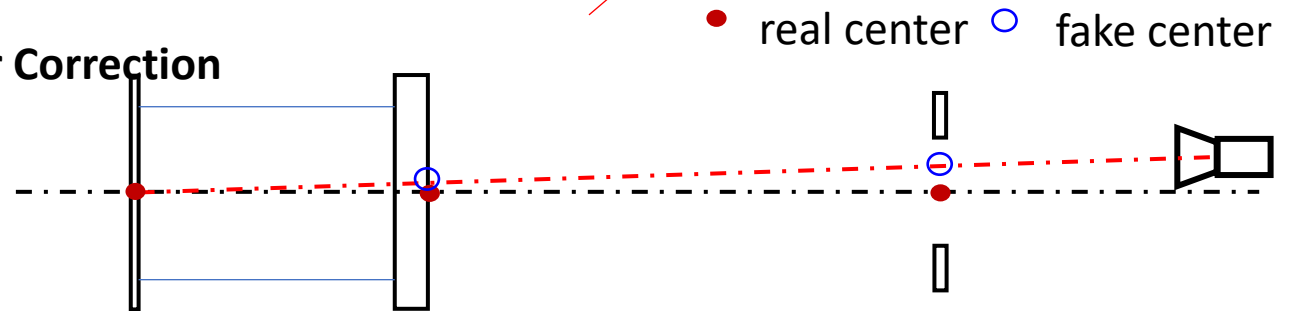
Perspective correction



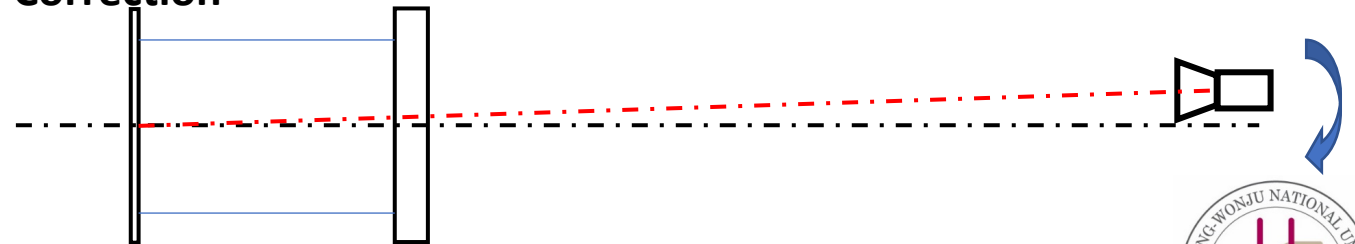
Ideal optics



Center Correction

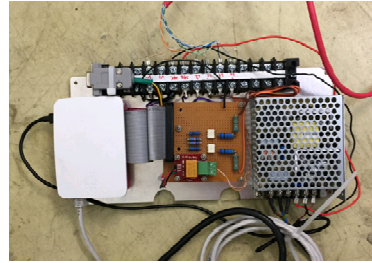


Rotate Correction

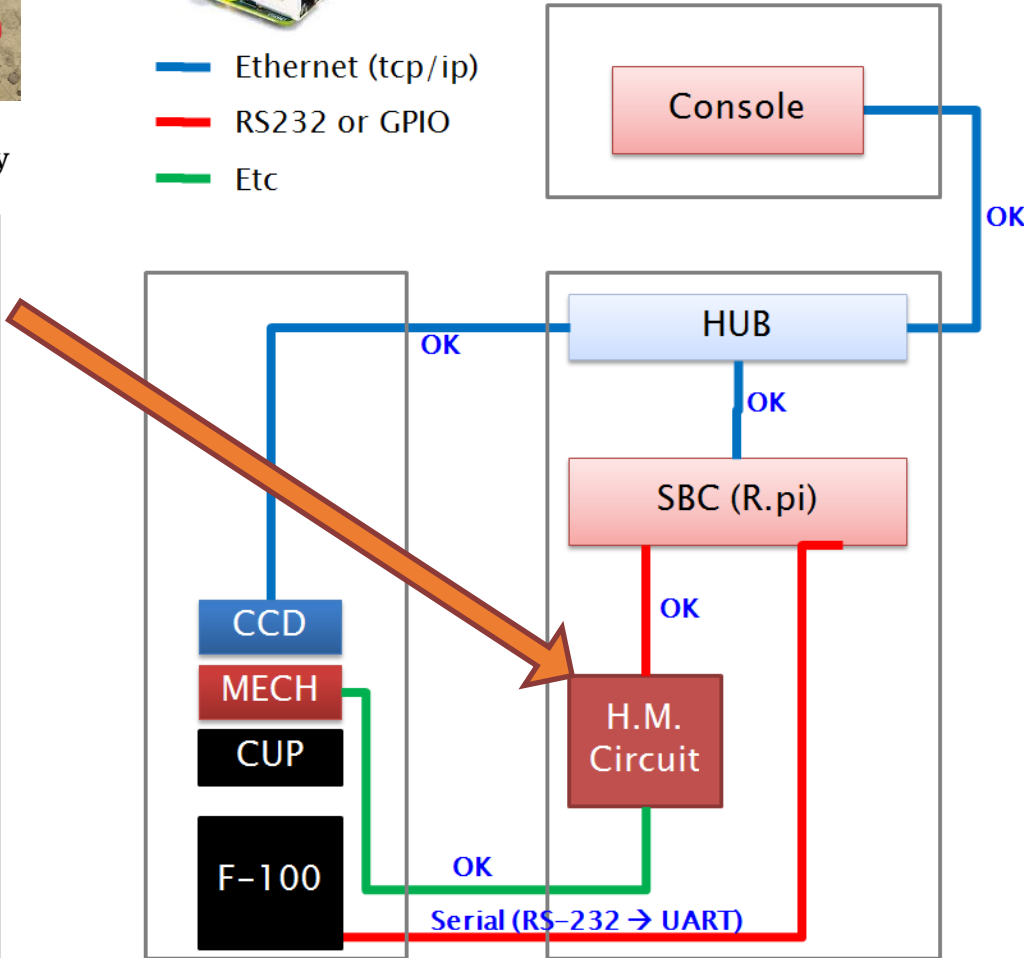
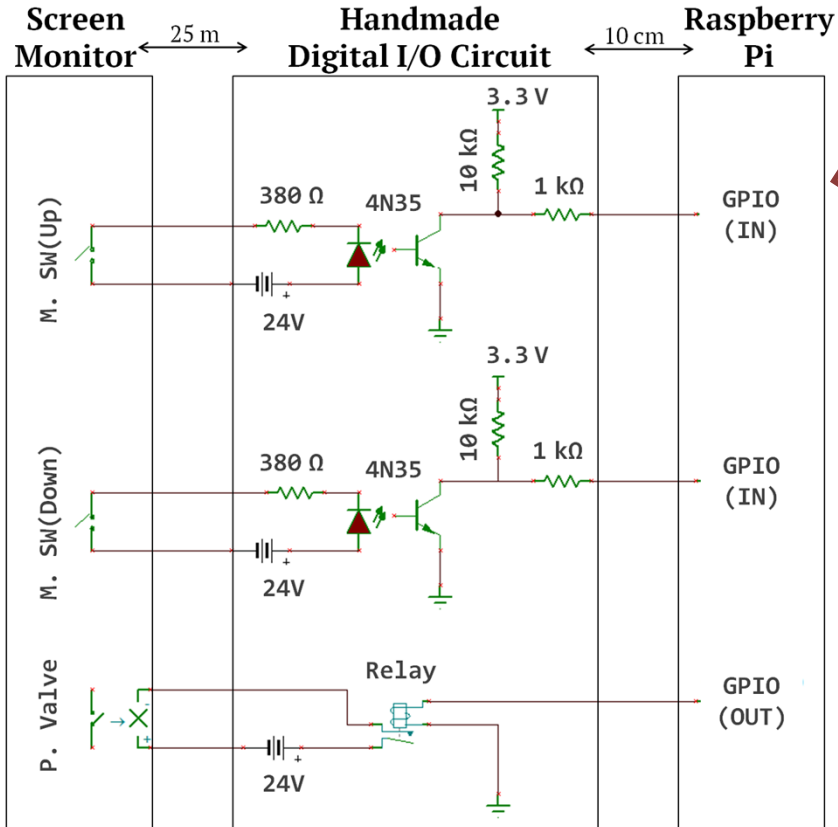


Control system

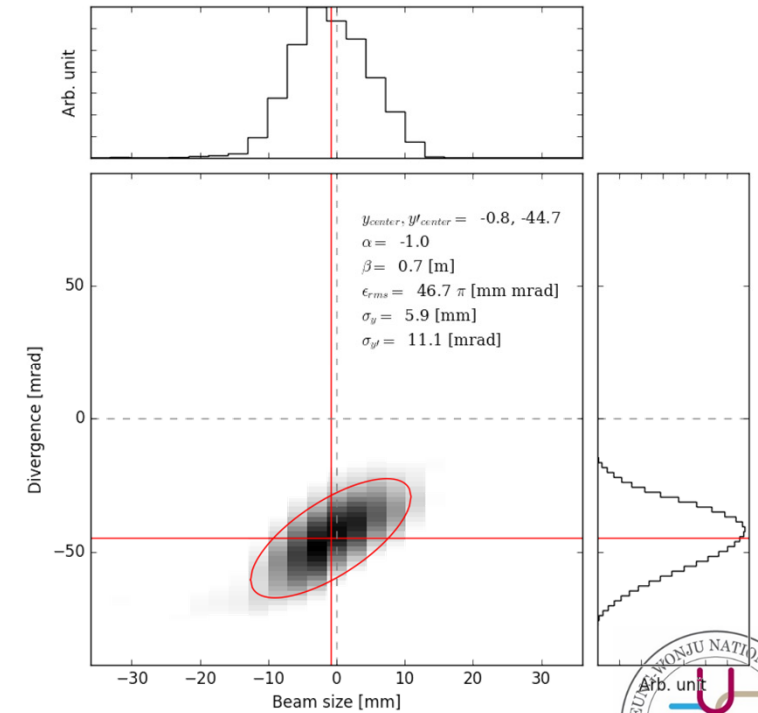
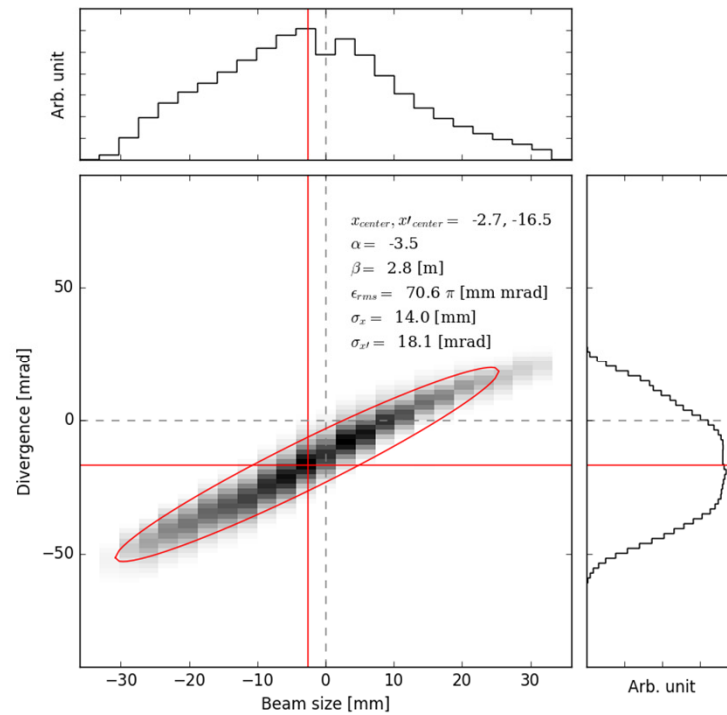
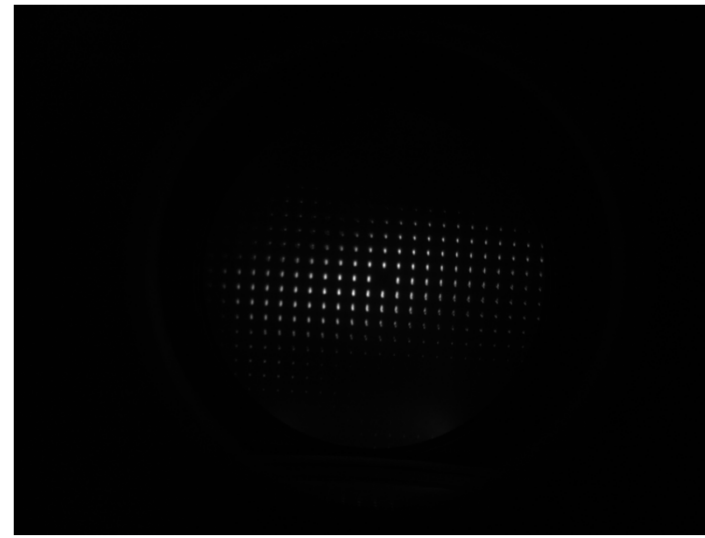
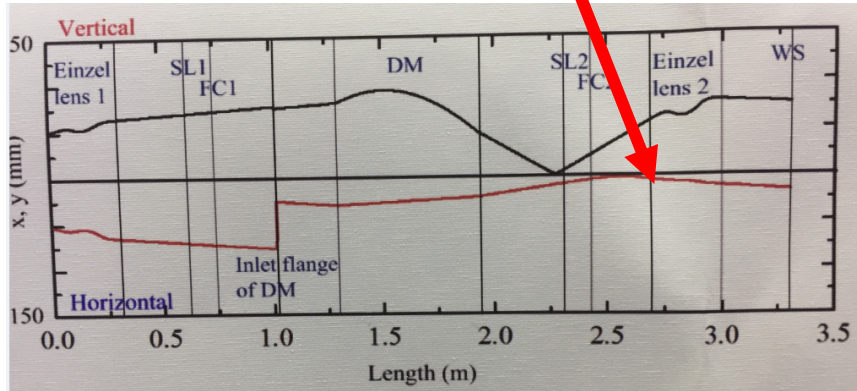
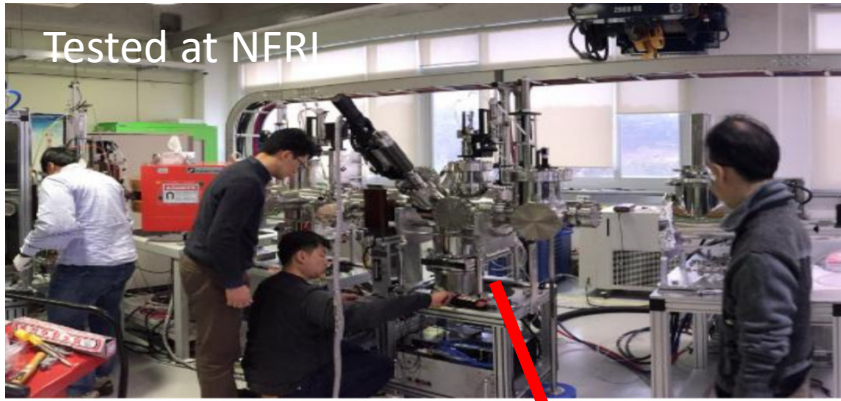
To save budget,
Handmade Circuit
was used
instead of PLC



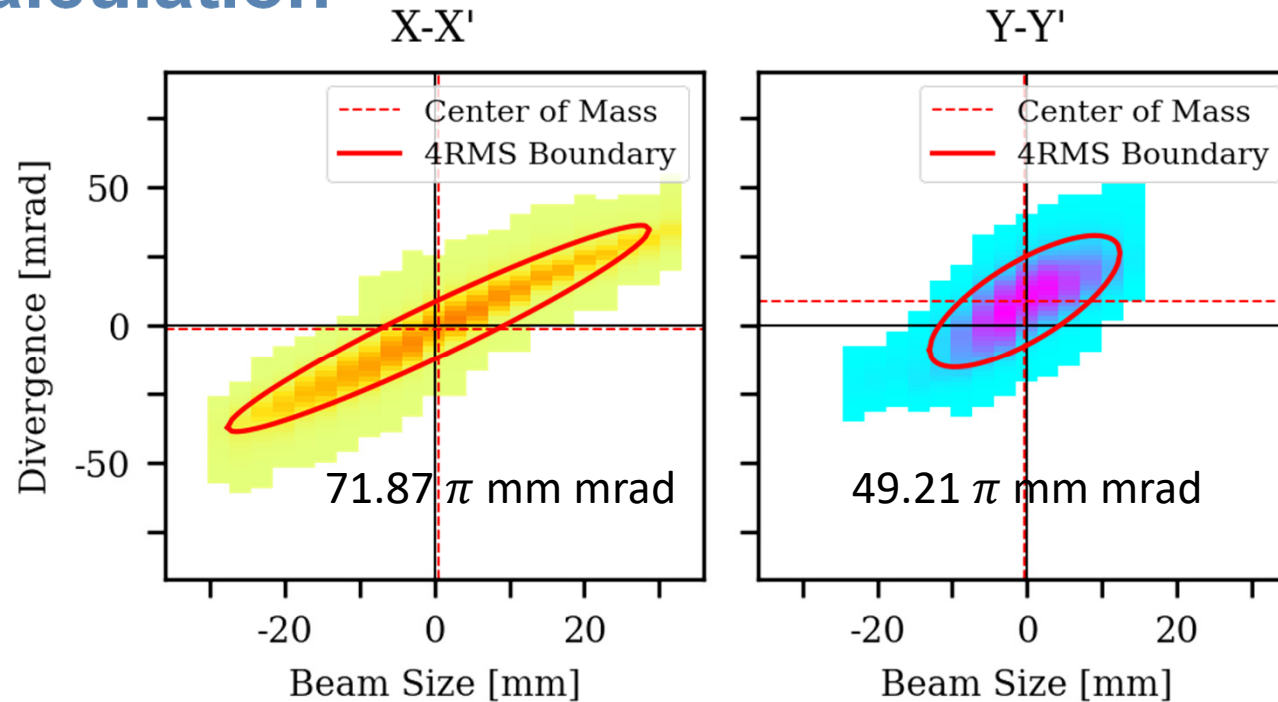
- Ethernet (tcp/ip)
- RS232 or GPIO
- Etc



Beam experiments



4D emittance calculation



RMS emittance

$$\epsilon_{\mu} = \sqrt{\langle \mu\mu \rangle \langle \mu'\mu' \rangle - \langle \mu\mu' \rangle^2}$$

$$C = \begin{bmatrix} \langle xx \rangle & \langle xx' \rangle & \langle xy \rangle & \langle xy' \rangle \\ \langle x'x \rangle & \langle x'x' \rangle & \langle x'y \rangle & \langle x'y' \rangle \\ \langle yx \rangle & \langle yx' \rangle & \langle yy \rangle & \langle yy' \rangle \\ \langle y'x \rangle & \langle y'x' \rangle & \langle y'y \rangle & \langle y'y' \rangle \end{bmatrix} = \begin{bmatrix} 181.41 & 231.83 & 31.55 & 13.51 \\ 231.83 & 324.85 & 44.63 & 24.00 \\ 31.55 & 44.63 & 36.48 & 50.37 \\ 13.51 & 24.00 & 50.37 & 135.30 \end{bmatrix}$$

Statistical Twiss parameter

$$\alpha_{\mu} = -\frac{\langle \mu\mu' \rangle}{\epsilon_{\mu}}, \quad \beta_{\mu} = \frac{\langle \mu\mu \rangle}{\epsilon_{\mu}}$$

$$\langle \mu\nu \rangle = \frac{\sum_i \sum_j \iint W_{i,j}(x', y') \mu\nu dx' dy'}{\sum_i \sum_j \iint W_{i,j}(x', y') dx' dy'}$$

Summary



The pepper-pot instrument is widely used at low-energy beams since it is capable of a single-shot measurement of 4D emittance + coupling terms.

For gauging a beam emittance accurately, pepper-pot diagnostics have to be carefully designed in terms of

- Precise mask production (**lithography + SEM**)
- Noise subtraction algorithm (**cluster removal**)
- Rotation correction (**perspective correction**)

In this study, we validated the mask fabrication process by SEM and the effectiveness of the cluster removal algorithm by virtual images as well as beam experiments. Contrary to other filters, the cluster removal algorithm is able to suppress noise without distortion on the signal.

Thank you for your attention

