

# X-ray FEL Lays the Groundwork for Scandium-45 Nuclear Clock

*Yuri Shvyd'ko*

Free Electron Laser Conference FEL2024  
August 18-23, 2024 – Warsaw, Poland

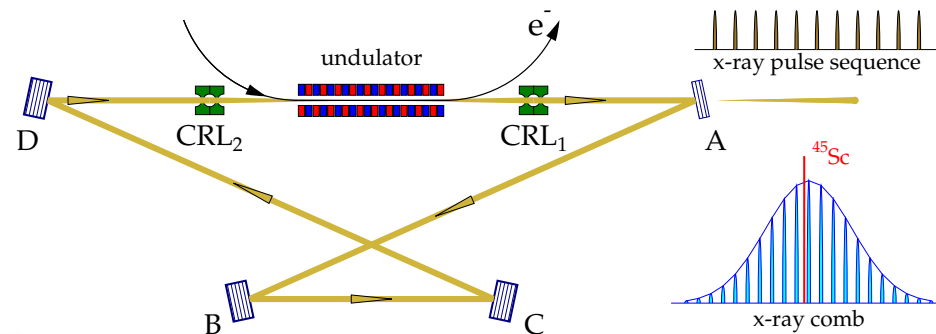
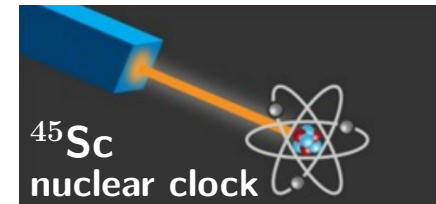
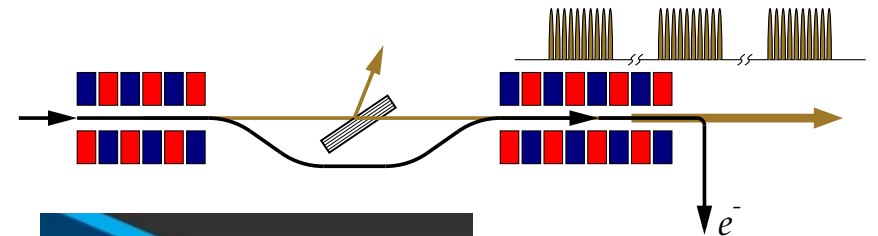


Warsaw Clock Tower

# Brief Introduction to Scandium-45

- $^{45}\text{Sc}$  nuclei exhibit an extraordinary narrowband  $\Gamma_o(^{45}\text{Sc}) \simeq 1.4 \text{ feV} = 1.4 \times 10^{-15} \text{ eV}$  x-ray resonance transition with transition energy  $E \simeq 12.4 \text{ keV}$  and with exceptionally large quality factor  $Q = E/\Gamma_o(^{45}\text{Sc}) \simeq 10^{19}$ .
- It has succeeded in driving this extremely sharp x-ray quantum transition with an x-ray source of highest average spectral brightness: a self-seeded high-repetition-rate XFEL.
- This opens up new horizons for exquisite applications such as nuclear clocks, extreme metrology, ultra-high-resolution spectroscopy, etc.
- These applications call for further development of the XFEL technology towards XFEL oscillators (XFELo) and x-ray combs.

$$\frac{\Gamma_o(^{57}\text{Fe})}{\Gamma_o(^{45}\text{Sc})} = \frac{4.8 \text{ neV}}{1.4 \text{ feV}} \simeq 3 \times 10^6$$



# Content

- Atomic and nuclear frequency standards.
- $^{45}\text{Sc}$  as a nuclear frequency standard and XFELs.
- Resonant x-ray excitation of  $^{45}\text{Sc}$ .
- Next steps.
- Summary.

Nature | Vol 622 | 19 October 2023 | **471**

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**Article**

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## Resonant X-ray excitation of the nuclear clock isomer $^{45}\text{Sc}$

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<https://doi.org/10.1038/s41586-023-06491-w>

Received: 15 May 2023

Accepted: 27 July 2023

 Check for updates

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# <sup>45</sup>Sc Collaboration

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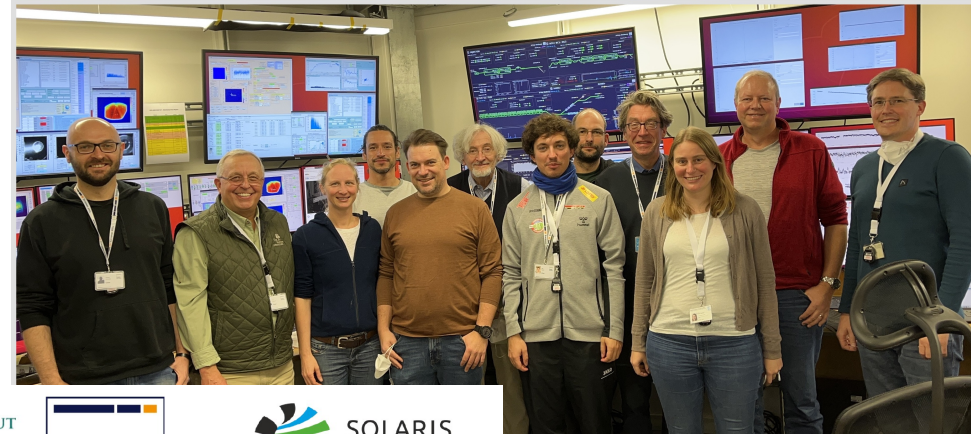
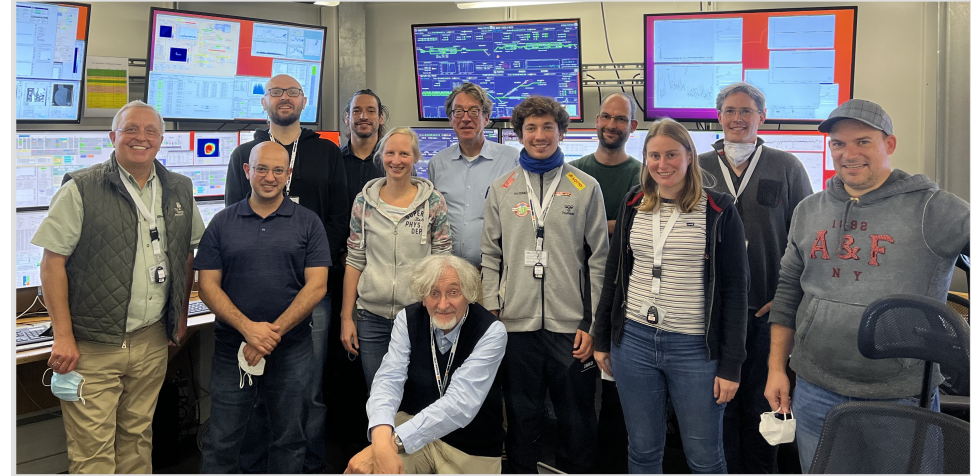
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Hans-Christian Wille  
Ilya Sergeev  
Christian Grech  
Marc Guetg  
Vitali Kocharyan  
Shan Liu  
Weilun Qin

## Solaris, Krakow

Tomasz Kolodziej





# Frequency Standards Enable Time Measurements

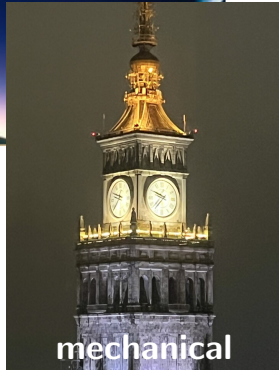
Oscillators with stable frequencies and large quality factors – frequency standards – determine our ability to keep track of time. Atomic clocks are presently our most precise measurement devices.

They define the second; enable GPS; test fundamental principles of physics with highest precision ...



celestial

$10^{-2}$



mechanical

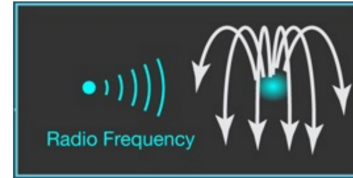
$10^{-4}$

solid state

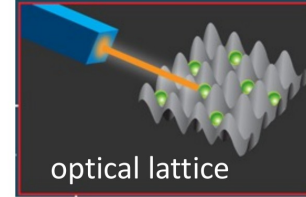


$10^{-6}$

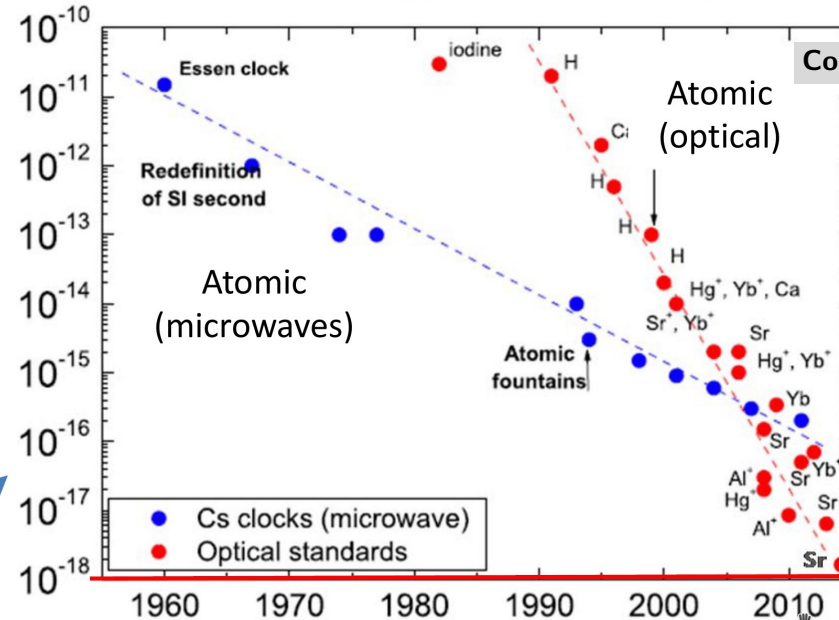
fractional uncertainty



Radio Frequency



optical lattice



Courtesy of Ralf Röhlsberger

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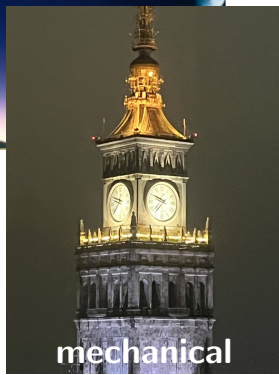
# Frequency Standards Enable Time Measurements

Oscillators with stable frequencies and large quality factors – frequency standards – determine our ability to keep track of time. Atomic clocks are presently our most precise measurement devices.

Search for more accurate, stable, and convenient reference oscillators is ongoing.



$10^{-2}$



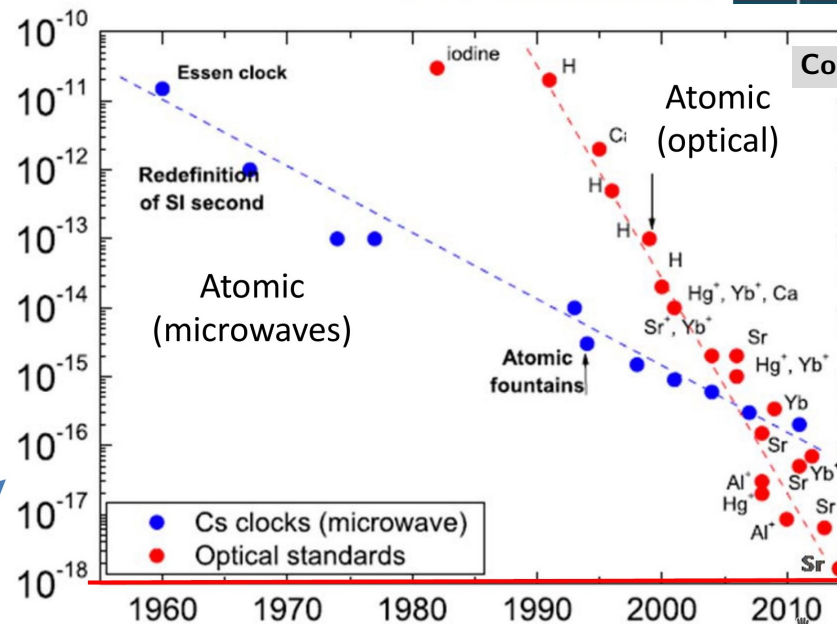
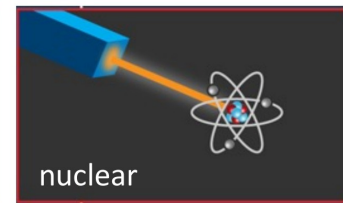
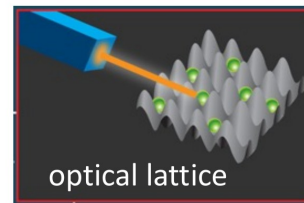
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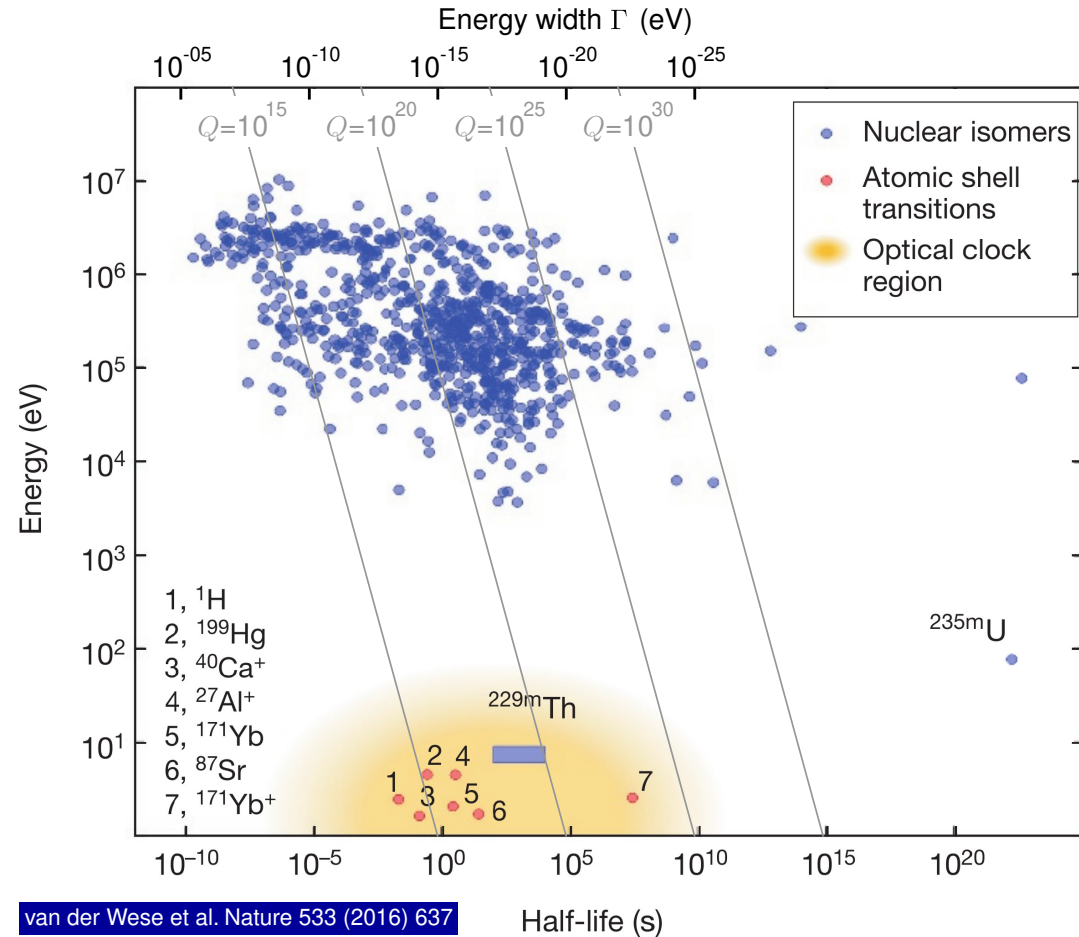
Courtesy of Ralf Röhlsberger

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# Nuclear vs. Atomic Resonances

1. **Higher Q-factors.**  $Q = E/\Gamma$
2. **Higher frequency:** a higher-frequency transition offers greater stability for simple statistical reasons (fluctuations are averaged over more cycles).
3. **Insensitivity to environmental effects.** Due to its small size, small magnetic moments, and the shielding effect of the surrounding electrons, an atomic nucleus is much less sensitive to ambient electromagnetic fields than is an electron in an orbital.
4. **Macroscopic number of atoms can be used,** because of the insensitivity to ambient fields, it is not necessary to have the clock atoms well-separated in a dilute gas or in ion traps at very low temperatures.
5. **Mössbauer effect with nuclei in solids** would allow solid-state amount of nuclei to exhibit narrow spectral resonance line at moderately-low temperatures.

E Peik, et al. "Nuclear clocks for testing fundamental physics" *Quantum Sci. Technol.* 6 (2021) 034002



# Nuclear Clock Isomer $^{229m}\text{Th}$

$$\Gamma_o(^{229m}\text{Th}) \sim 10^{-18} \text{ eV}$$

A lot of effort was dedicated to studies of the  $^{229m}\text{Th}$  isomer and to accurate measurements of the nuclear transition energy: 8.338(24) eV [\*].

L. van der Wese et al. Nature 533 (2016) 637  
"Direct detection of the  $^{229m}\text{Th}$  nuclear clock transition"

Masuda, T. et al. Nature 573, 239 (2019)  
X-ray pumping of the  $^{229m}\text{Th}$  nuclear clock isomer.

Seiferle, B. et al. Nature 573, 243 (2019)  
Energy of the  $^{229m}\text{Th}$  nuclear clock transition.

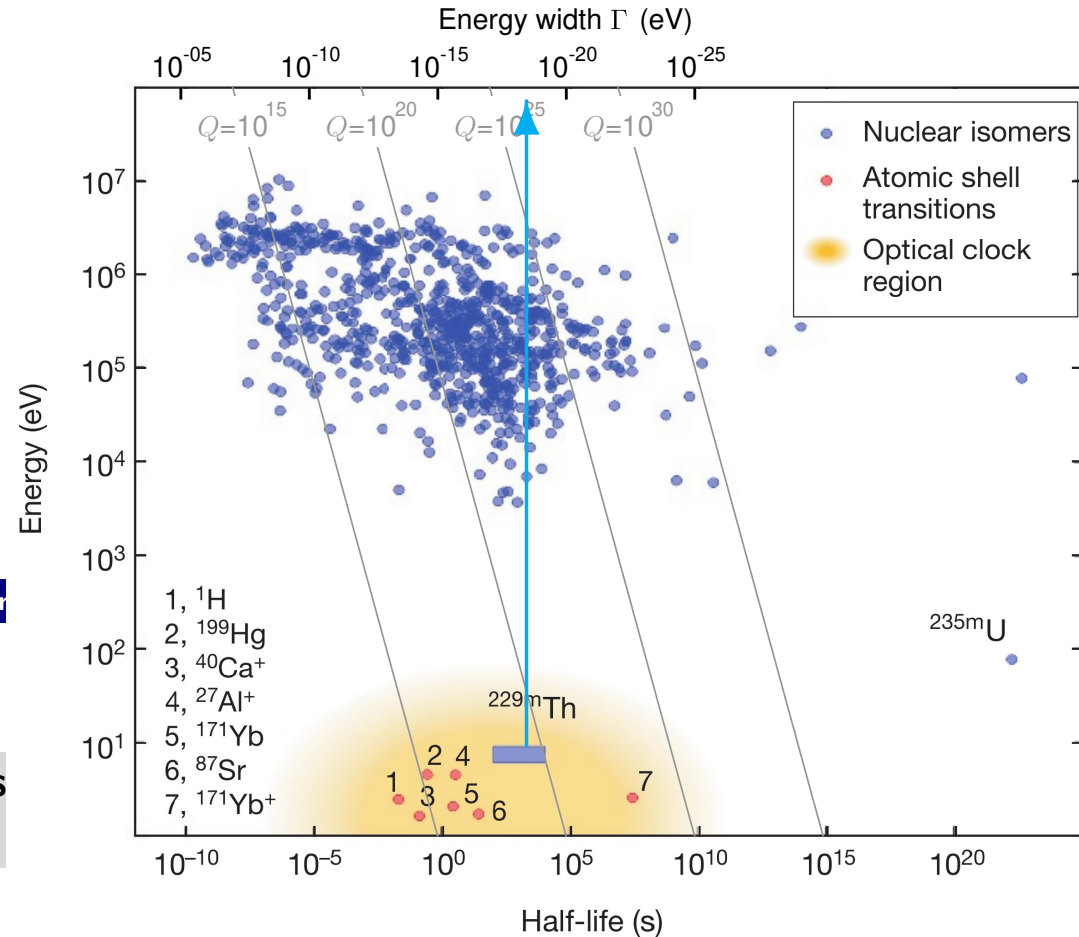
Sikorsky, T. et al. Phys. Rev. Lett. 125, 142503 (2020)  
Measurement of the  $^{229m}\text{Th}$  isomer energy with a magnetic microcalorimeter

[\*] Kraemer, S. et al. Nature 617, 706 (2023)  
Observation of the radiative decay of the  $^{229m}\text{Th}$  nuclear clock isomer.

Excitation of the  $^{229m}\text{Th}$  resonance with photons was achieved very recently: 8.355733(10) eV

[\*\*] J. Tiedau, Peik E. et al. Phys. Rev. Lett. 132 (2024) 182501

[\*\*] R. Elwell, E. Hudson et al. Phys. Rev. Lett. 133 (2024) 013201

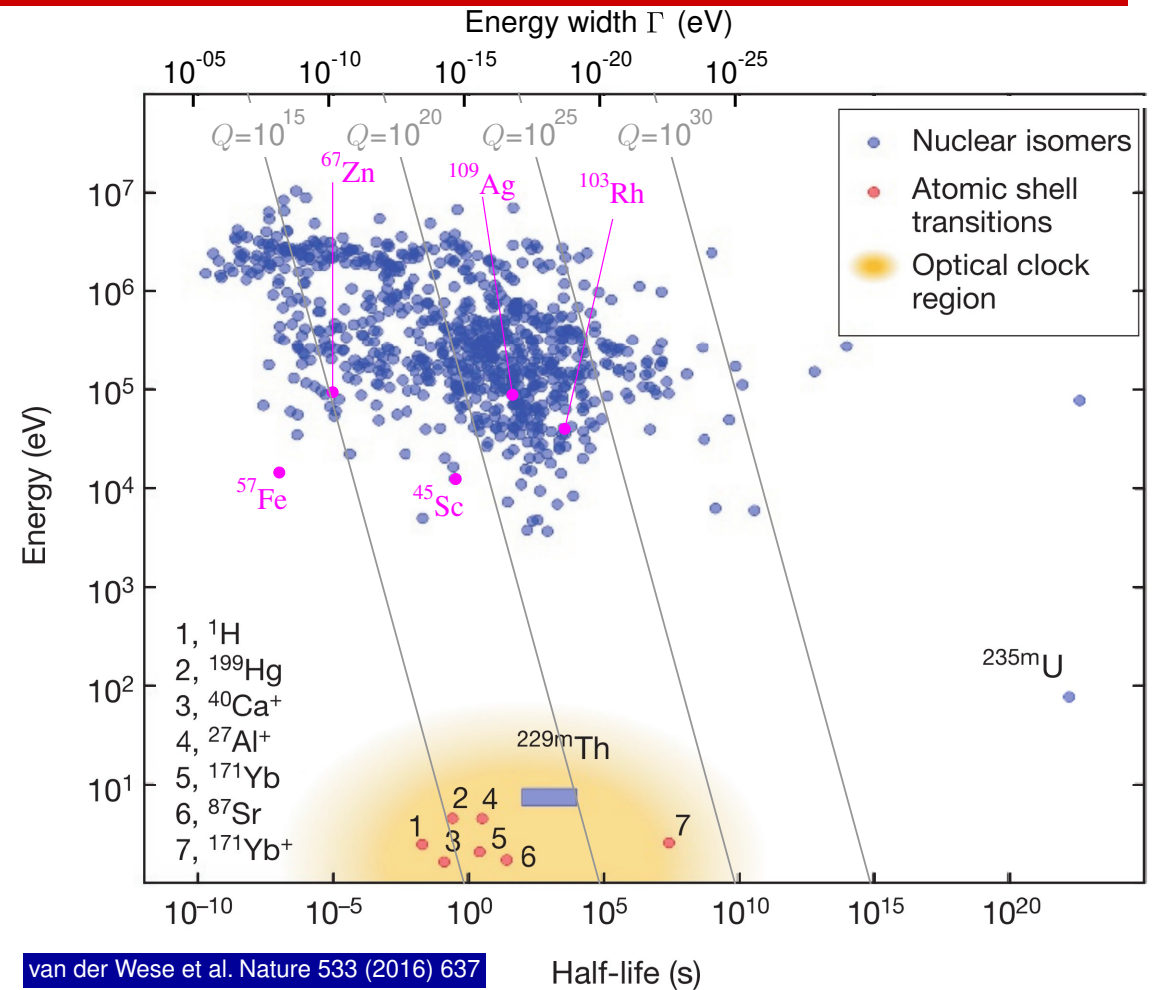




# Other Candidates for Nuclear Clocks

Most of the nuclear isomers (with stable ground states) have the excitation energy above 30 keV ( $^{67}\text{Zn}$ ,  $^{109}\text{Ag}$ ,  $^{119}\text{Rh}$ ) and therefore cannot be driven by the modern coherent sources of electromagnetic radiation.

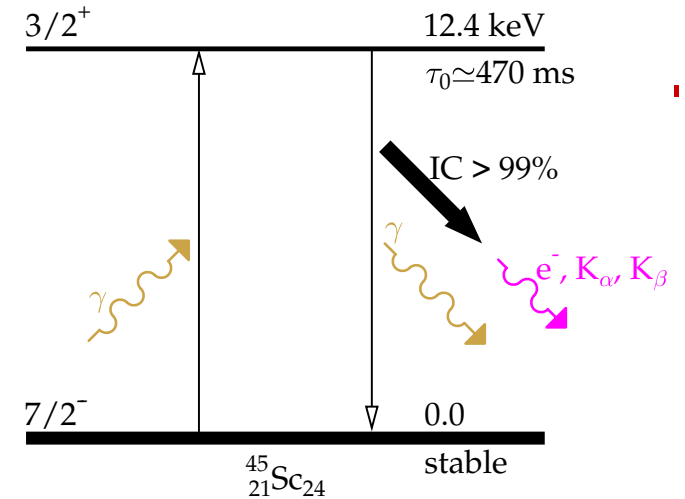
Fortunately, along with  $^{229\text{m}}\text{Th}$  there is another notable exception –  $^{45}\text{Sc}$ .



# 12.4-keV Nuclear Resonance of $^{45}\text{Sc}$

## Basic Features

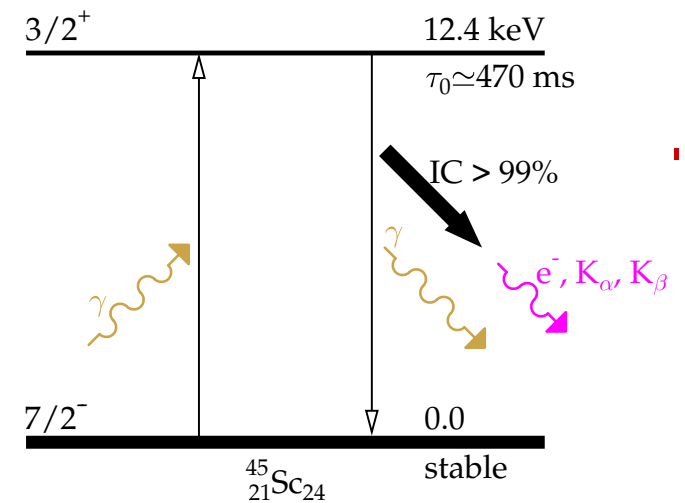
Excitation energy:  $E = 12.40 \pm 0.05$  keV, [1,2,3,6]  
excited state lifetime:  $\tau = 0.47$  s, [1,5,6]  
natural energy width:  $\Gamma_0 = \hbar/\tau = 1.4 \times 10^{-15}$  eV = 1.4 feV,  
resonance quality:  $Q = E/\Gamma_0 \simeq 10^{19}$ ,  
**internal conversion coefficient:  $\alpha \simeq 630$** , [4,5,6]  
 $^{45}\text{Sc}$  natural abundance: 100%,  
gravitational red shift: 1 mm/ $\Gamma_0$ ,  
room temperature Lamb-Mössbauer factor:  $f_{\text{LM}} \simeq 0.8$ .



- [1] Holland R.E., Lynch F.J., Nystén K.E., PRL 13 (1964) 241-243.
- [2] Freedman, M. S., Porter, F. T. & Wagner F.Jr, Phys. Rev. 140, B563-B565 (1965).
- [3] Porter, F. T., Freedman, M. S., Wagner F., & Orlandini, K. A., Phys. Rev. 146, 774-780 (1966).
- [4] Jones, K. W. and Schwarzschild, Phys. Rev. 148, 1148-1150 (1966).
- [5] Blaugrund, A. E., Holland, R. E. & Lynch, F. J., Phys. Rev. 159, 926-930 (1967).
- [6] Burrows, T. W., Nuclear Data Sheets 109, 171-296 (2008).

# 12.4-keV Nuclear Resonance of $^{45}\text{Sc}$ History in Brief

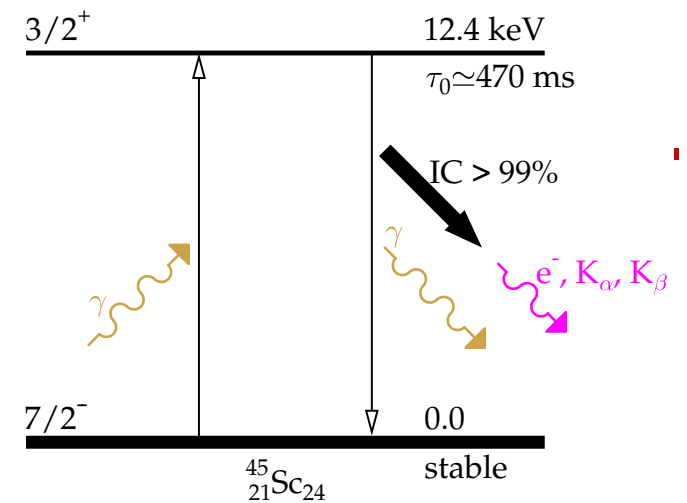
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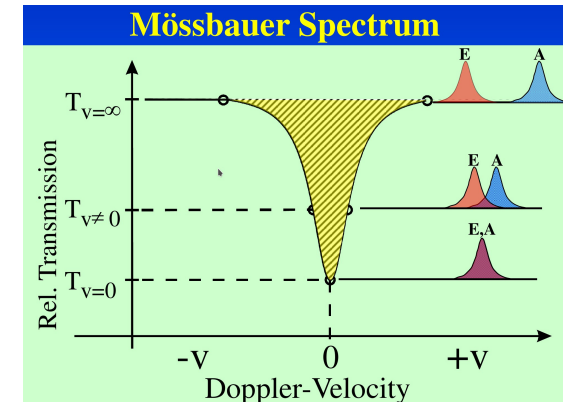
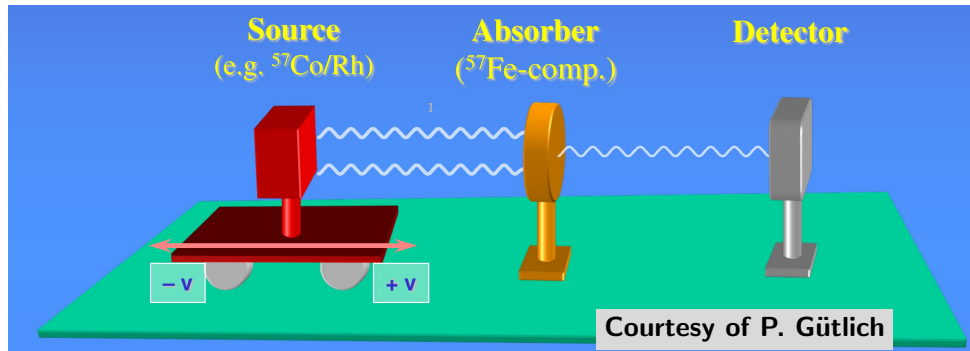
- A 13-keV gamma-emitting state of **0.44-sec mean lifetime** was found in  $^{45}\text{Sc}$  by  $(p, p')$  reaction on  $^{45}\text{Sc}$  at Argonne National Laboratory in 1964. **R.E. Holland, F.J. Lynch, K.E. Nystén, PRL 13 (1964) 241-243**

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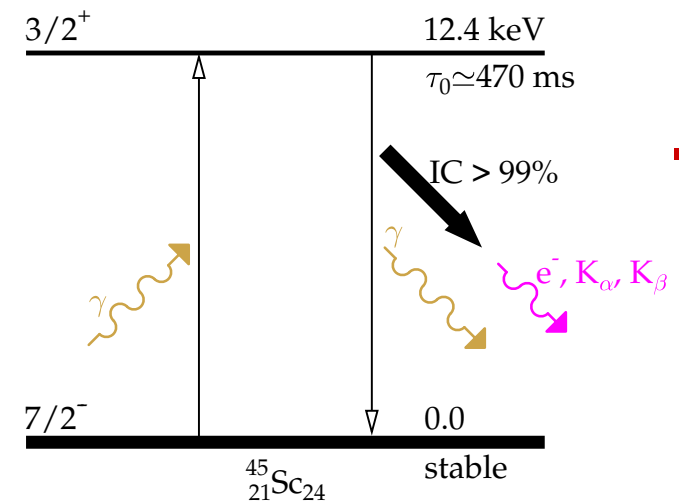
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  - Unfortunately,  $^{45}\text{Sc}$  does not have any convenient parent radioactive source.
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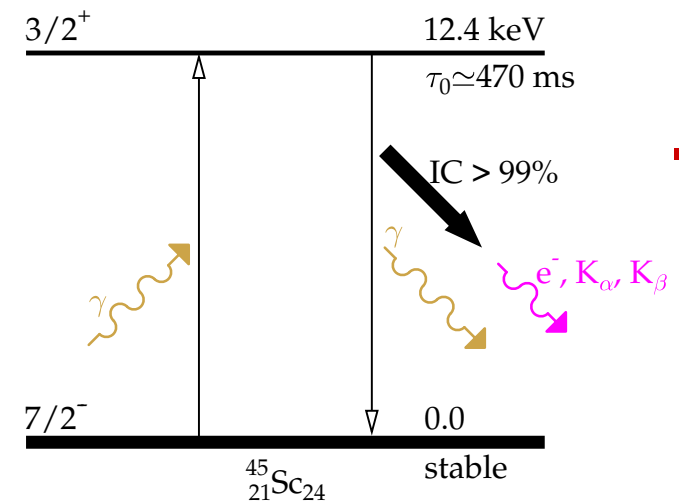
- $^{45}\text{Sc}$  was rediscovered and resurrected in 1990:

- (1) resonant excitation of  $^{45}\text{Sc}$  is feasible using 12.4-keV x-rays from **accelerator-based x-ray sources** of high spectral brightness and flux, which started to emerge in 1990s (ESRF, APS, SPring-8);

- (2) spectral width of the long-lived state can be accessed by measuring **time dependence of coherent nuclear-resonant forward scattering (NFS)** **Yu. Shvyd'ko and G.V. Smirnov NIM 51 (1990) 452-457.**

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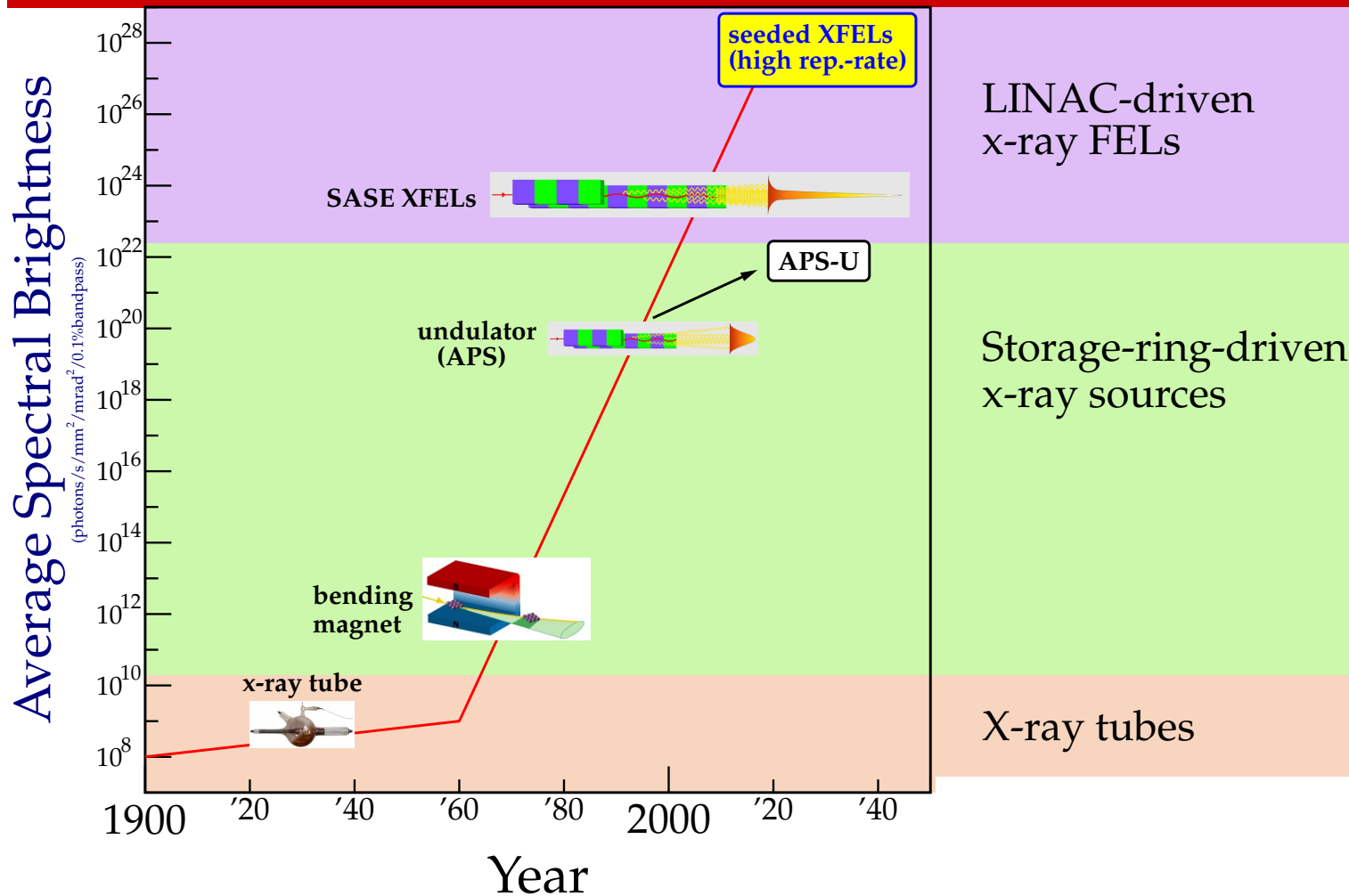
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- Attempts to detect the  $^{45}\text{Sc}$  resonance at 3rd-generation synchrotron radiation sources (ESRF, APS, SPring-8) were so far unsuccessful. Spectral flux was still low.

# History of Hard X-ray Spectral Brightness



- Simultaneously, there was a remarkable progress with XFELs in the past two decades.

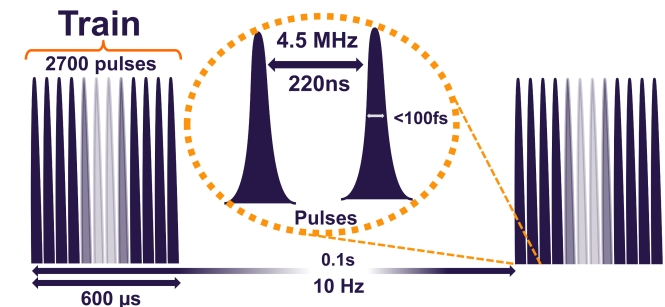
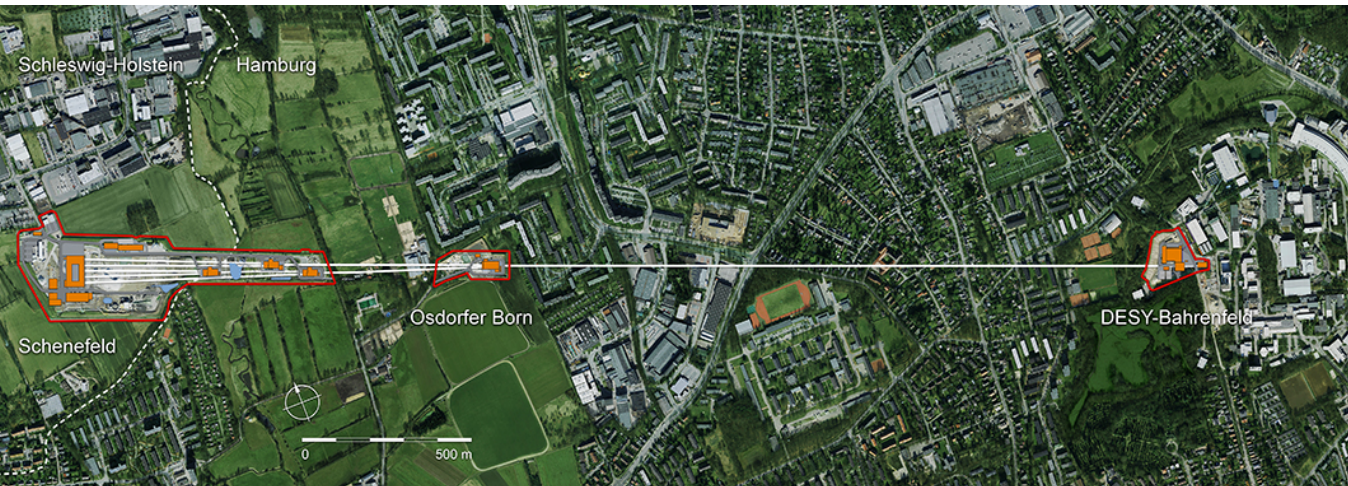
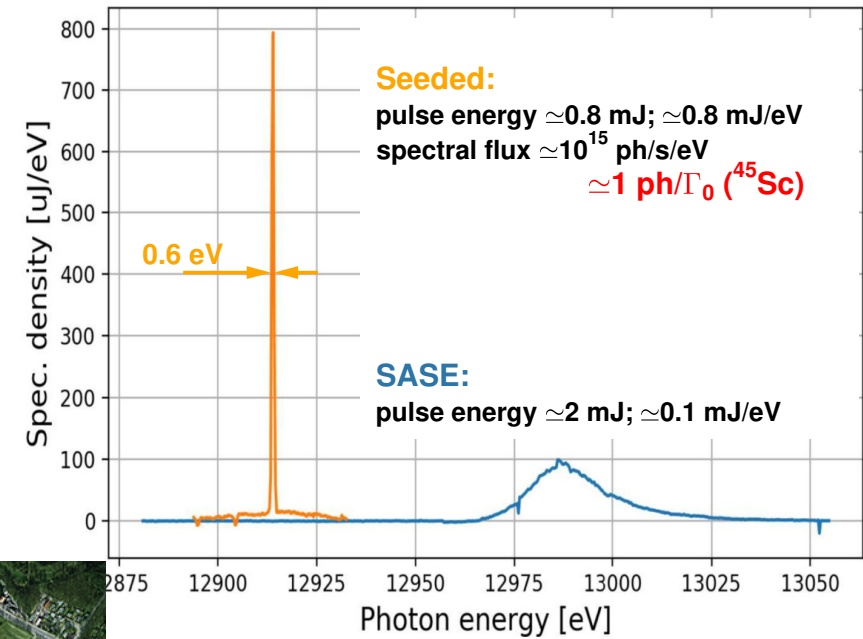
- The most advanced hard XFELs – self-seeded (HXRSS) high-repetition-rate (HRR) XFELs – may provide average spectral flux >1000 than ESRF, APS, SPring-8, or PETRA-III undulators.

O. Chubar et al., JSR 23 (2016) 410

- HXRSS HRR XFELs may provide sufficient spectral flux to drive <sup>45</sup>Sc resonance.

# $^{45}\text{Sc}$ Experiment at European XFEL (Hamburg, Germany)

- European XFEL is the 1st high rep.-rate XFEL  
W. Decking, et al. Nat. Photonics, 14 (2020) 391.
- An average spectral flux at 13 keV of up to  $\approx 10^{15}$  ph/s/eV  $\approx 1$  ph/ $\Gamma_0(^{45}\text{Sc})$  was demonstrated in self-seeded mode S. Liu et al. Nature Photonics 17 (2023) 984.
- European XFEL has a unique time structure suitable perfectly for the detection of the  $^{45}\text{Sc}$  resonance: sub-ms pulse trains with a 100-ms dark time.

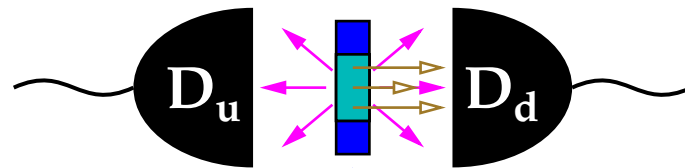




# $^{45}\text{Sc}$ Experiment in a Nutshell: Highest Spectral Flux – Lowest Detector Background

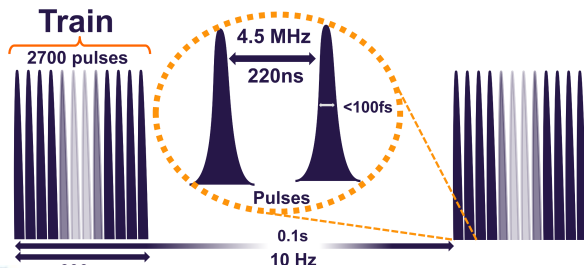
With a 25- $\mu\text{m}$  thick **Sc metal** target exposed to an x-ray beam with  $\simeq 1 \text{ ph/s}/\Gamma_0 \simeq 10^{15} \text{ ph/s/eV}$ , the expected count-rate in  $D_1$  or  $D_2$  of 4-keV  $K_{\alpha,\beta}$ -fluorescence is 1-5 ph/100 s.

$\rightarrow K_{\alpha,\beta} \simeq 4 \text{ keV} \quad \rightarrow \text{NFS} = 12.4 \text{ keV}$

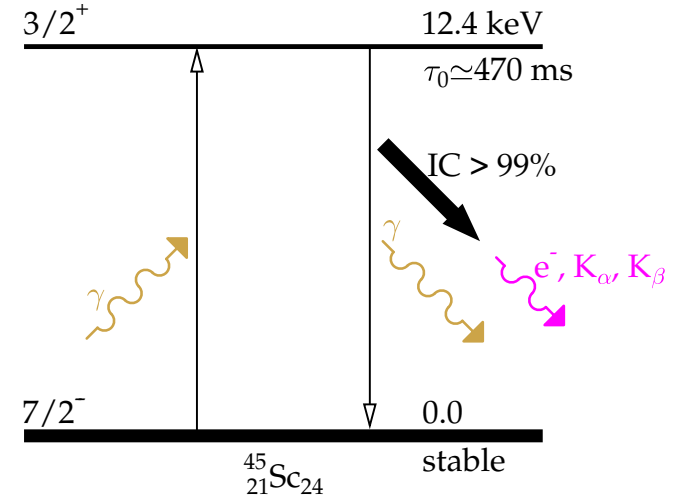


100 ms

12.4-keV x-rays

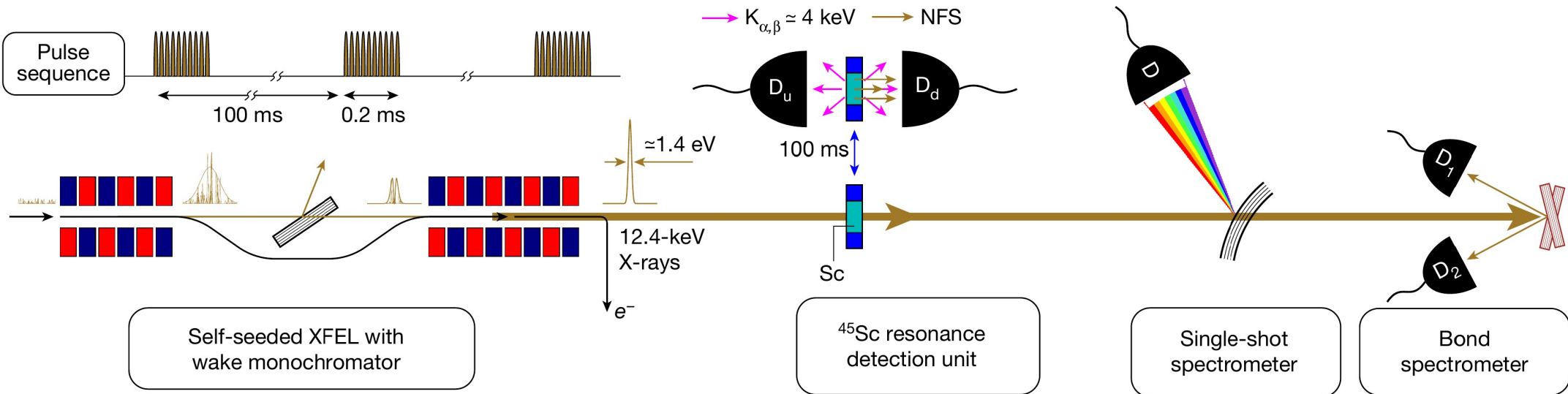


Sc

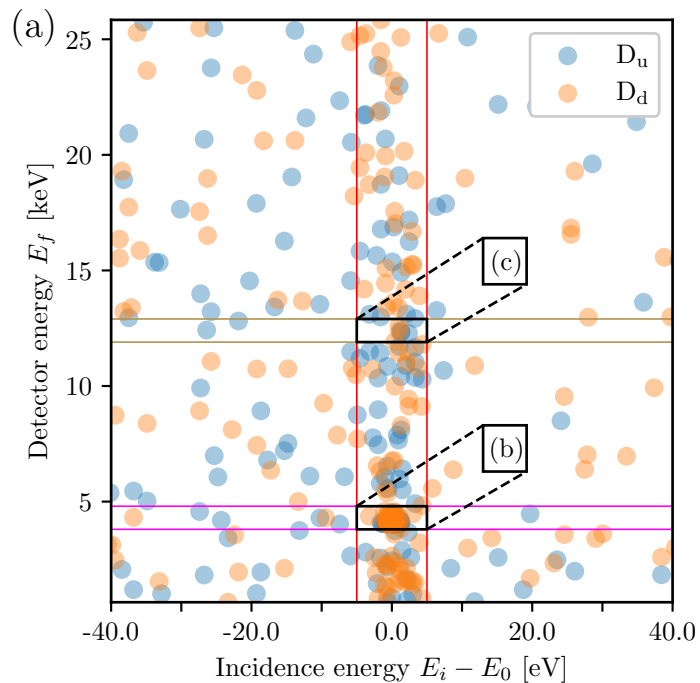


Detection of the nuclear decay products with time, spatial, energy, and polarization discrimination ensures very low detector noise floor **<2 counts/10000 s**.

# Experimental Setup and Experiment Execution



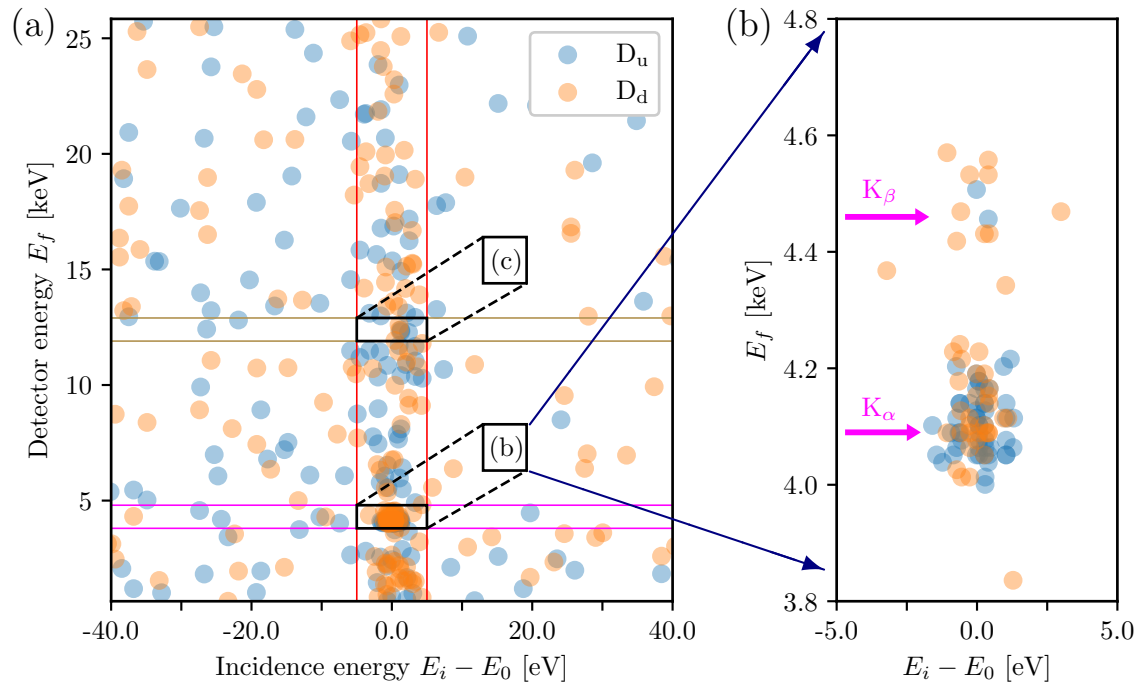
# $^{45}\text{Sc}$ Resonance Detected - 2D Picture



- XFEL photon energy  $E_i$  was scanned in a  $\pm 50$  eV range around 12.4 keV.
- $\simeq 10^{20}$  of 12.4-keV photons were directed to Sc targets.

(a) Counts from the  $D_u$  and  $D_d$  x-ray detectors plotted as the energy  $E_f$  of the detected X-ray photons versus incident X-ray photon energy  $E_i - E_0$ . The photons were recorded in a time window of  $\simeq 20$ -80 ms after every pulse-train excitation.

# $^{45}\text{Sc}$ Resonance Detected - 2D Picture



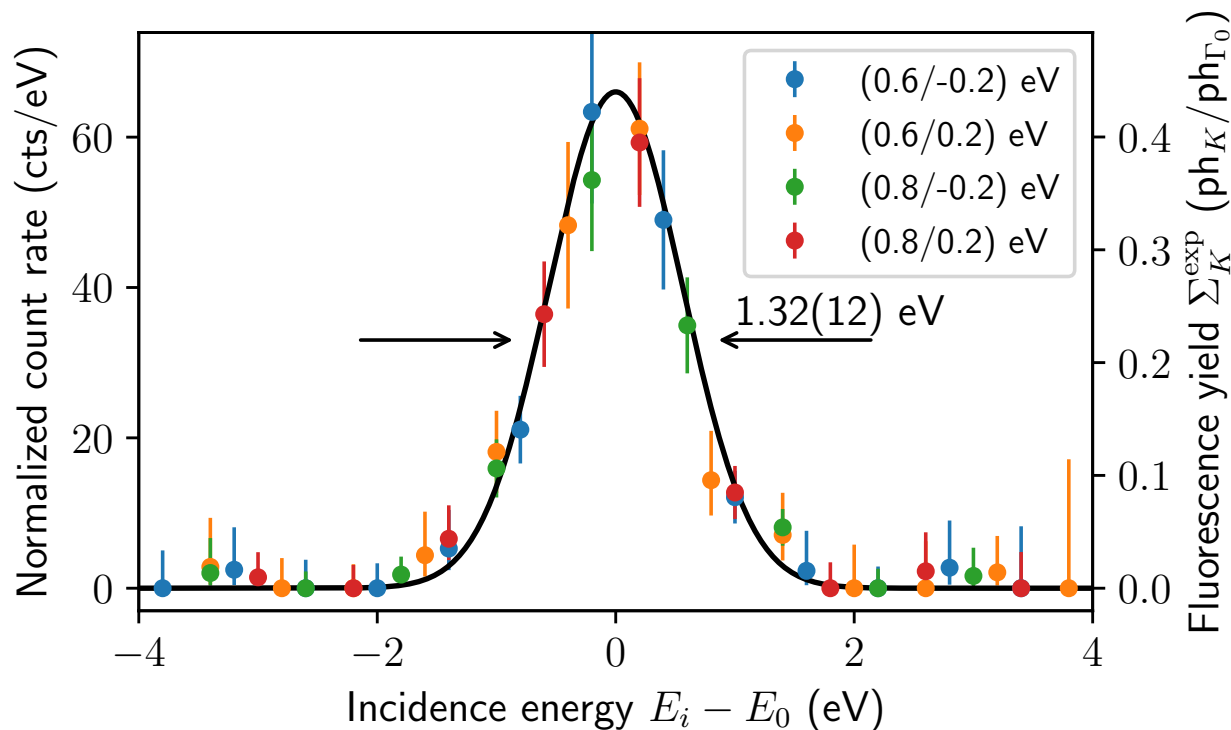
- XFEL photon energy  $E_i$  was scanned in a  $\pm 50$  eV range around 12.4 keV.
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- $\simeq 93$  of 4-keV  $K_{\alpha,\beta}$ -fluorescence photons were detected with a  $>20$ -ms delay.
- Signal to noise ratio  $\simeq 70$ .

(a) Counts from the  $D_u$  and  $D_d$  x-ray detectors plotted as the energy  $E_f$  of the detected X-ray photons versus incident X-ray photon energy  $E_i - E_0$ . The photons were recorded in a time window of  $\simeq 20$ -80 ms after every pulse-train excitation.

(b) Close-up of the 4.3-keV ROI, showing two clusters of counts centered at the energies of Sc  $K_\alpha$  (4.09 keV) and  $K_\beta$  (4.46 keV) fluorescence as a direct confirmation of detection of the  $^{45}\text{Sc}$  resonance.

# $^{45}\text{Sc}$ Resonance Detected & Resonance Energy Determined



The  $^{45}\text{Sc}$  nuclear resonance transition energy  $E_0$  previously known to an uncertainty of  $\simeq \pm 50$  eV, was determined with more than a hundred times higher accuracy as

$$E_0 = 12,389.59^{+0.15(\text{stat})}_{+0.12(\text{syst})} \text{ eV}$$

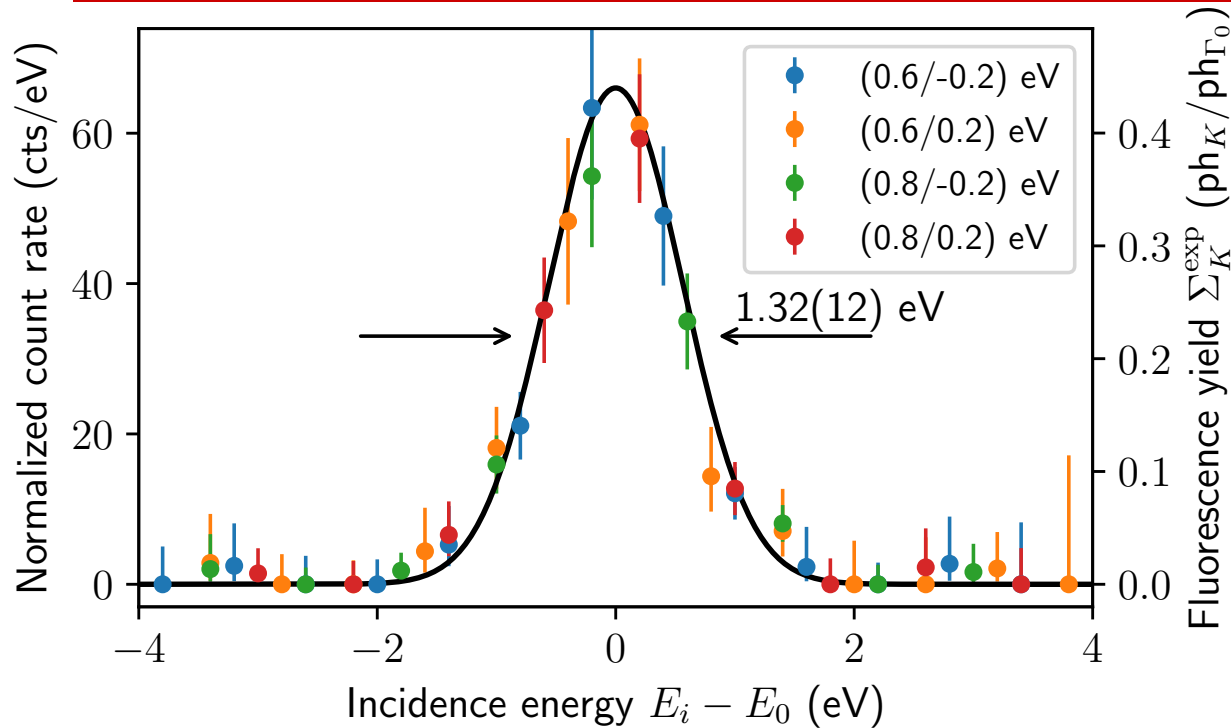
using Bond technique.

Time-delayed  $^{45}\text{Sc}$  K-shell fluorescence as a function of incoming X-ray photon energy  $E_i$  relative to resonance energy  $E_0$ .

The spectral width of 1.32(12) eV reflects the spectral width of the incoming XFEL radiation. The colored dots are exemplary binned data.



# $^{45}\text{Sc}$ Internal Conversion Coefficients $\alpha$ & $\alpha_K$ and Nuclear Resonance Cross-section $\sigma_0$ Refined



The measured **nuclear-resonance-assisted K-shell fluorescence yield**  $\Sigma_K^{\text{exp}} = 0.44(10) \text{ ph}_K/\text{ph}_\Gamma$  for one incident resonant photon within  $\Gamma_0$  is in a 100% disagreement with the value calculated with a theory, which uses published IC coefficients [3-5].

Parameter		Magnitude
Energy	$E_0$	12,400(50) eV [1,2,5]
		12,389.59 $^{\pm 0.15(\text{stat})}_{+0.12(\text{syst})}$ eV
Internal conversion (IC) coefficients	$\alpha, \alpha_K$	632(71), 474 [3,4,5] 424, 363 [6]
Cross section	$\sigma_0$	$1.26(15) \times 10^{-20} \text{ cm}^2$
		$1.9(5) \times 10^{-20} \text{ cm}^2$

A good agreement with the experiment is achieved with IC coefficients predicted by the **state-of-the-art internal conversion theory** [6]. The resonant cross-section  $\sigma_0$  can be refined appropriately.

- [1] Freedman, M. S., et al., Phys. Rev. 140, B563-B565 (1965).
- [2] Porter, F. T., et al., Phys. Rev. 146, 774-780 (1966).
- [3] Jones, K. W. and Schwarzschild, Phys. Rev. 148, 1148-1150 (1966).
- [4] Blaugrund, A. E., et al., Phys. Rev. 159, 926-930 (1967).
- [5] Burrows, T. W., Nuclear Data Sheets 109, 171-296 (2008).
- [6] Kibedi, T., et al., NIM A 589, 202-229 (2008).

# What are the Next Steps with $^{45}\text{Sc}$ ?

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# $^{45}\text{Sc}$ Nuclear Forward Scattering to Determine the Actual Resonance Width

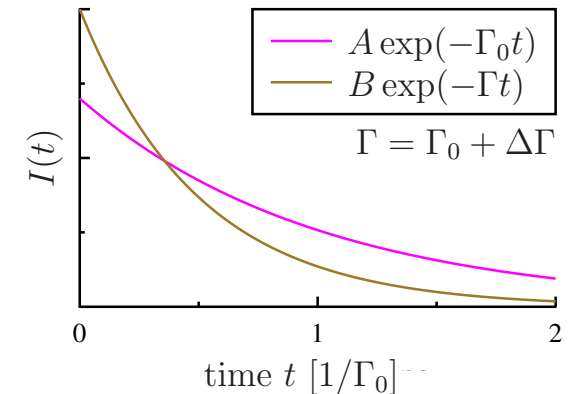
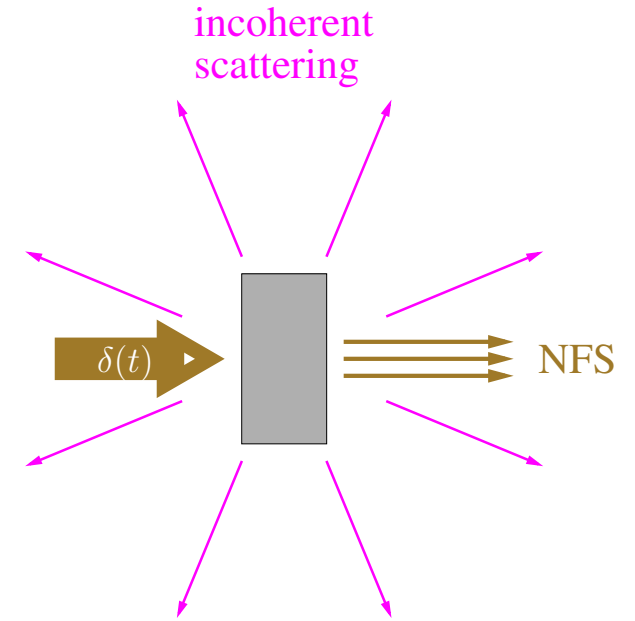
- We do not know the actual width  $\Gamma = \Gamma_0 + \Delta\Gamma$  of the  $^{45}\text{Sc}$  resonance in a solid state target, and how much is it broadened –  $\Delta\Gamma$  – compared to the natural linewidth  $\Gamma_0 = 1.4$  feV?

- Measuring  $\Gamma \simeq$  feV directly is a formidable challenge.

- Measuring complementary time dependences on the millisecond-scale instead of energy dependences on the feV-scale is a more straightforward approach.

- It requires measuring time dependence of **coherent** nuclear forward scattering (NFS) to access  $\Gamma$ .

Yu. Shvyd'ko and G.V. Smirnov NIM 51 (1990) 452-457



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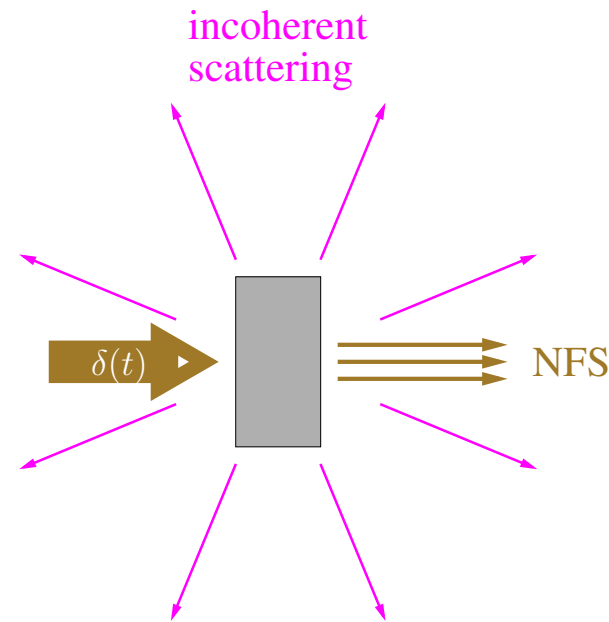
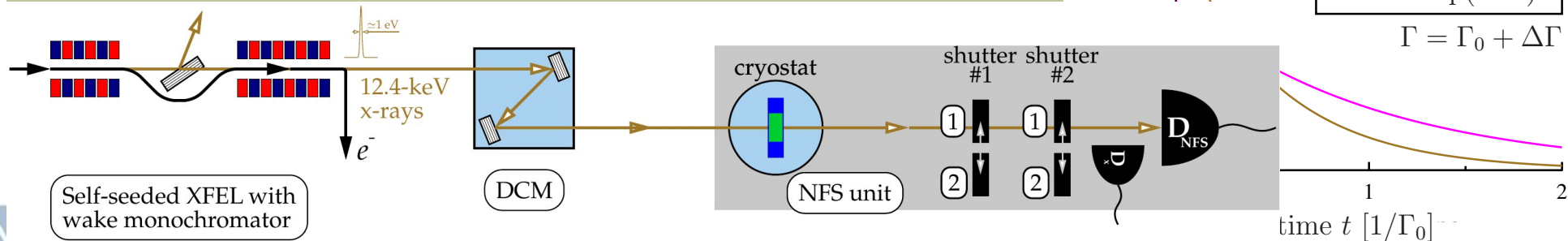
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The first  $^{45}\text{Sc}$  NFS experiment is planned for 2024 at EuXFEL.



# $^{45}\text{Sc}$ Nuclear Forward Scattering to Determine the Actual Resonance Width

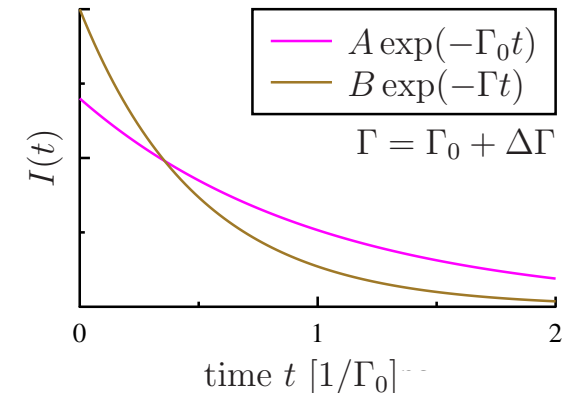
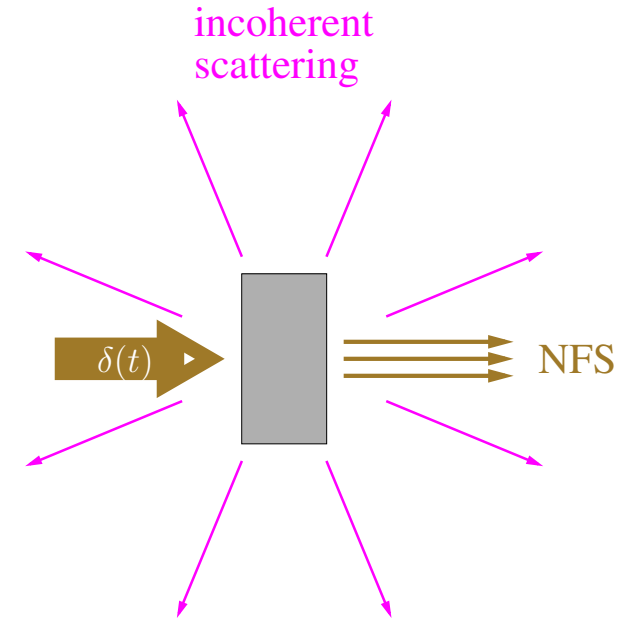
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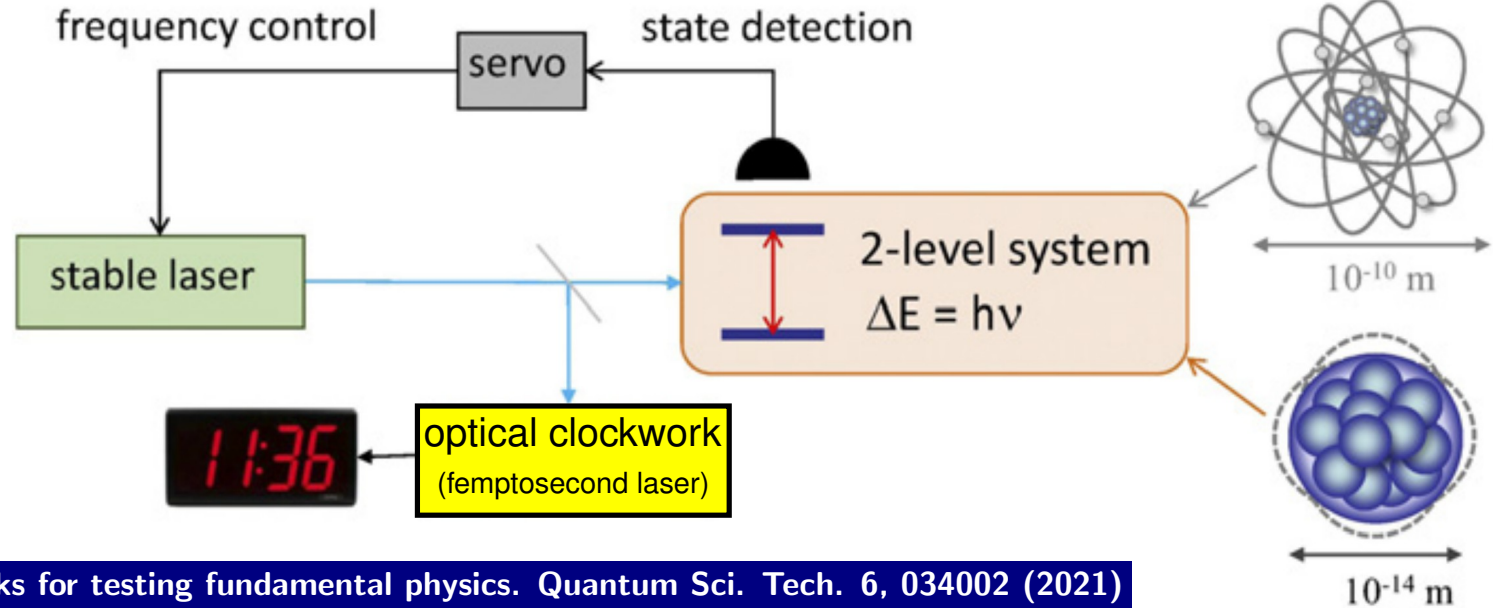
- It requires measuring time dependence of **coherent** nuclear forward scattering (NFS) to access  $\Gamma$ .

Yu. Shvyd'ko and G.V. Smirnov NIM 51 (1990) 452-457

- Observation of  $^{45}\text{Sc}$  NFS will not only allow us to determine  $\Gamma$ , but also enable important applications in ultra-high-precision coherent NFS spectroscopy, extreme metrology, etc. since the narrowness of the  $^{45}\text{Sc}$  resonance is expected to surpass all currently accessible Mössbauer resonances by orders of magnitude.



# Schematic of an Optical Atomic or Nuclear Clock



Peik, E. et al. Nuclear clocks for testing fundamental physics. *Quantum Sci. Tech.* 6, 034002 (2021)

The laser oscillator frequency is stabilized to the atomic or nuclear resonance frequency and an optical clockwork is employed to produce a time signal.

Realization of the  $^{45}\text{Sc}$  Mössbauer nuclear clock will require (1) a further increase of the resonant spectral flux using improved narrow-band 12.4-keV X-ray sources and (2) frequency combs stretching up to this energy.



# Path #1 to $^{45}\text{Sc}$ Mössbauer Nuclear Clock – HHG

- HHG inside a femtosecond enhancement cavity enables phase-coherent frequency combs in the XUV range:

R.J. Jones et al. Phys. Rev. Lett. 94, 193201 (2005).

A. Cingoz et al. Nature 482, 68–71 (2012).

- The intracavity HHG was extended into the XUV range with a spectral width of each harmonic of the order of 0.1 Hz:

C. Benko, et al. Nature Photonics, 8, 530–537 (2014).

This would perfectly match the spectral width of the  $^{45}\text{Sc}$  resonance.

- The cut-off photon energy in HHG has been pushed recently into the X-ray range (to 5.2 keV) from laser-induced multivalent ions of noble gas:

J. Gao et al. Optica 9, 1003–1008 (2022).

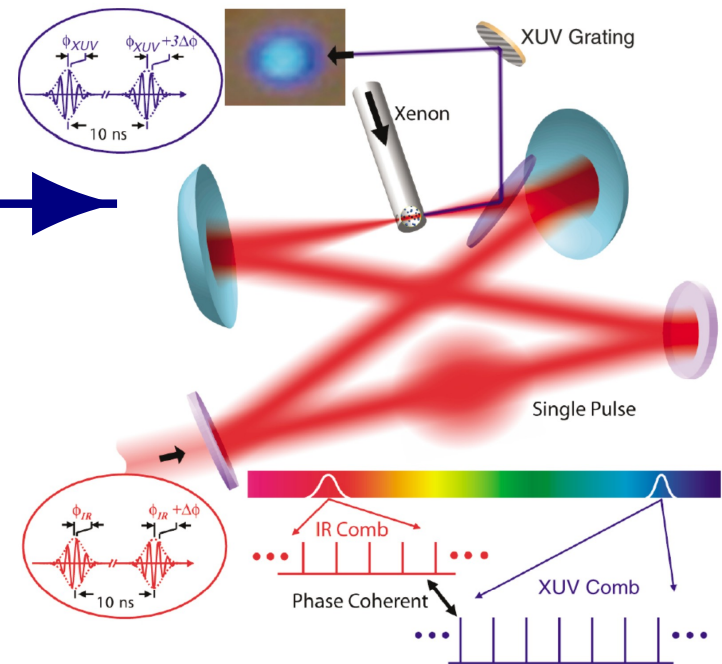


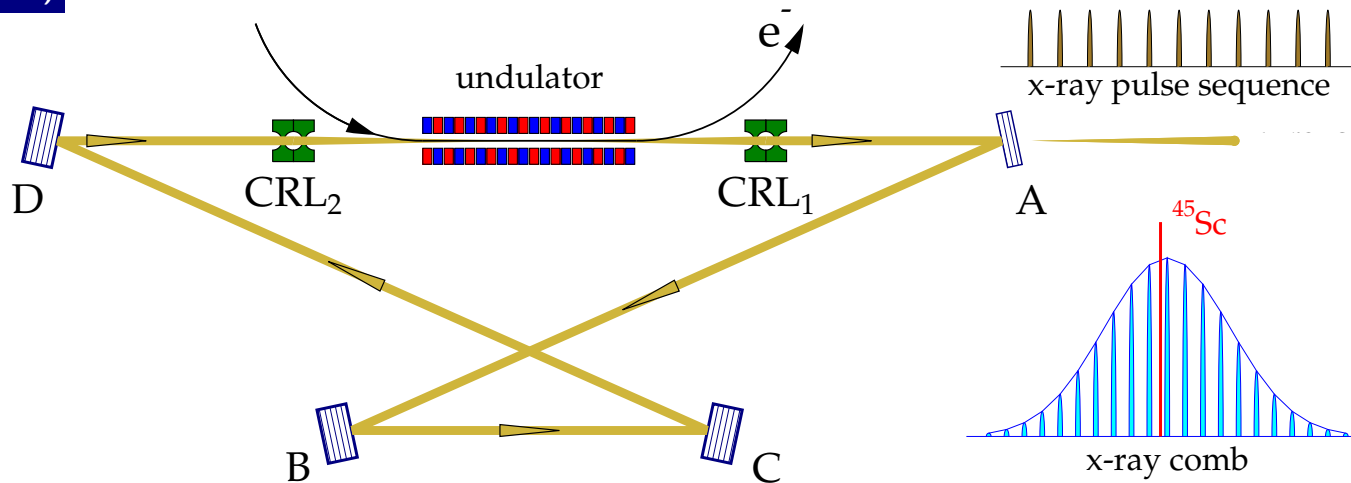
FIG. 1 (color). Schematic setup of intracavity high-harmonic generation. The incident pulse train is stabilized to a high finesse cavity, enhancing pulse energy nearly 3 orders of magnitude while maintaining a high repetition frequency. A gas target at the cavity focus enables phase-coherent HHG, resulting in a phase-stable frequency comb in the vacuum ultraviolet (VUV) spectral

# Path #2 to $^{45}\text{Sc}$ Mössbauer Nuclear Clock – XFELO

- X-ray free-electron-laser oscillator (XFELO) [1] and hard X-ray comb generated by a nuclear-resonance-stabilized XFELO [2].

[1] K.-J. Kim, Yu. Shvyd'ko, S. Reiche PRL 100, 244802 (2008)

[2] B. Adams and K.-J. Kim PRAB 18, 030711 (2015)



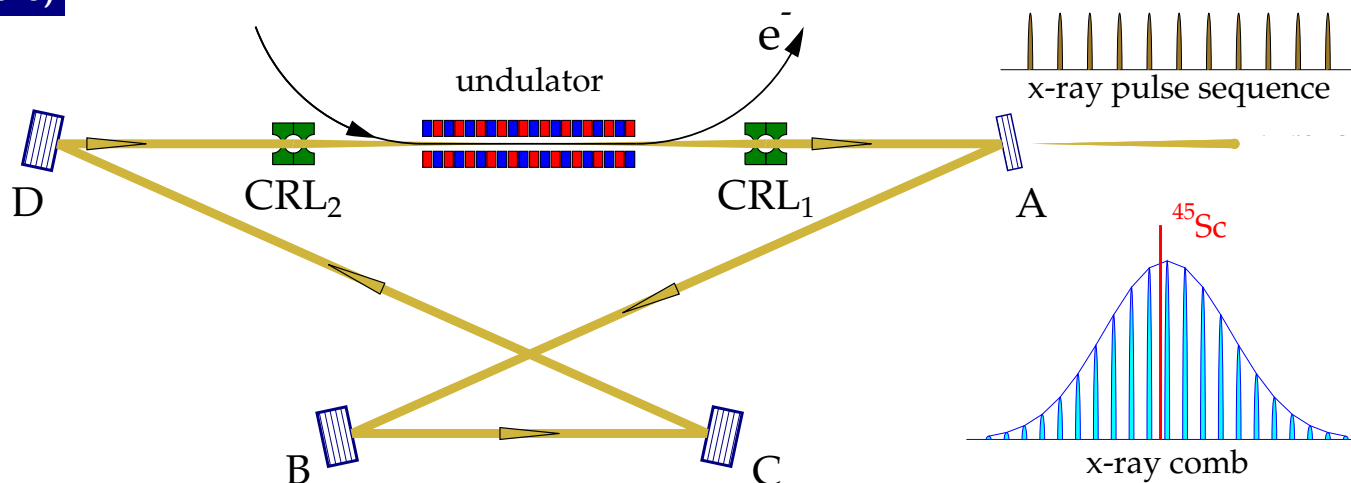
# Path #2 to $^{45}\text{Sc}$ Mössbauer Nuclear Clock – XFEL0

- X-ray free-electron-laser oscillator (XFEL0) [1] and hard X-ray comb generated by a nuclear-resonance-stabilized XFEL0 [2].

[1] K.-J. Kim, Yu. Shvyd'ko, S. Reiche PRL 100, 244802 (2008)

[2] B. Adams and K.-J. Kim PRAB 18, 030711 (2015)

- R&D on the realization of such devices is presently in progress at ANL/SLAC (USA) [3], at EuXFEL (Germany) [4], and is considered at SHINE (China) [5].



[3] G. Marcus et al., (2019) <https://doi.org/10.18429/JACoW-FEL2019-TUD04>

[4] P. Rauer et al., PRAB 26, 020701 (2023)

[5] N.-S. Huang et al., Nuclear Science and Techniques (2023) 34:6

# ANL-SLAC CBXFEL R&D Project (started 2019)

CBXFEL = Cavity-based XFEL

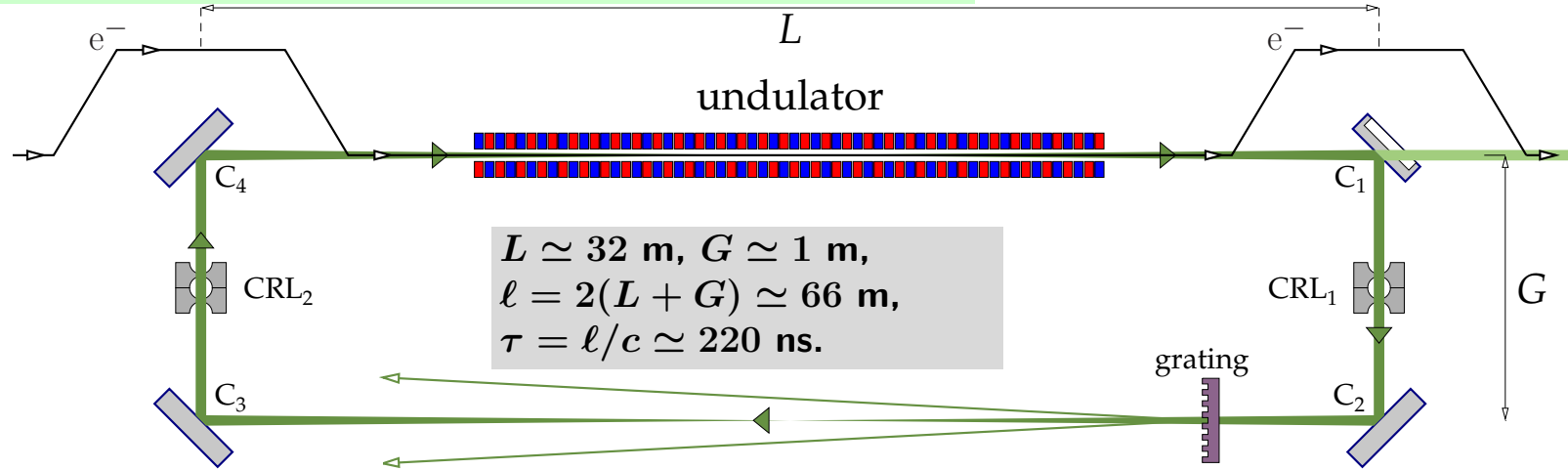
XFEL = low-gain CBXFEL

XRAFEL = high-gain CBXFEL



# ANL-SLAC CBXFEL R&D Project (started 2019)

1. Design, construct, and align a rectangular 4-crystal x-ray cavity (32-m long & 220-ns roundtrip-time) in the LCLS-II undulator hall at SLAC enclosing 7 undulator modules.

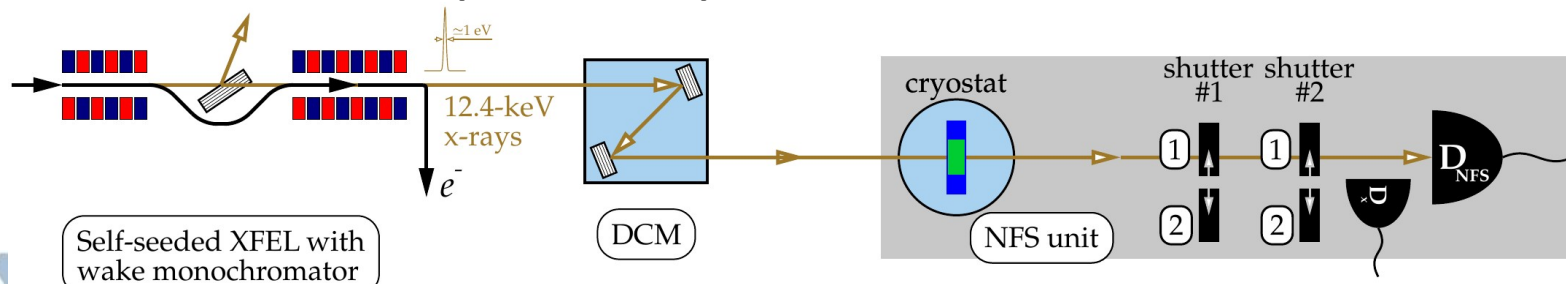


2. Perform 2-pass FEL gain in a 2-bunch cooper RF linac experiment as well as cavity ring-down measurements for both the low-gain XFEL and the high-gain XRAFEL schemes.

3. Demonstrate the x-ray optical cavity tolerance and stability requirements for future operation with the high repetition rate electron beam from a SCRF linac.

# Summary and Outlook

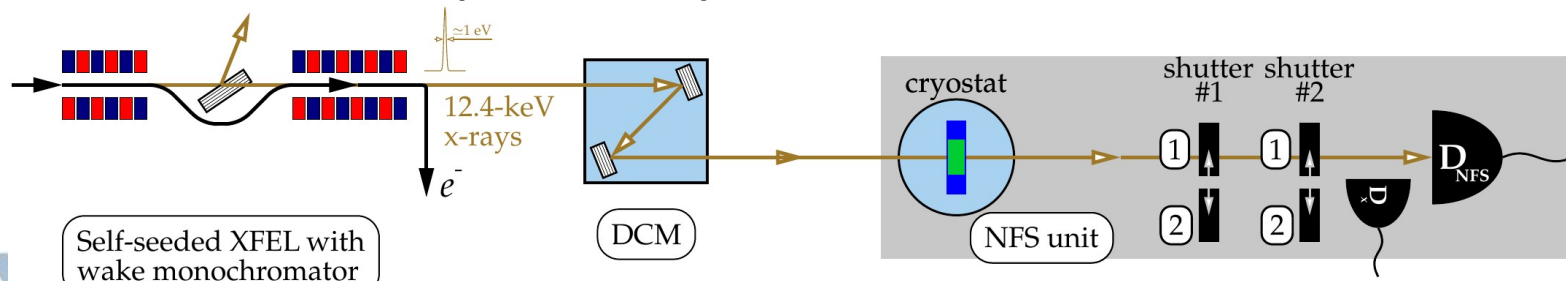
- The long-lived nuclear transition of  $^{45}\text{Sc}$  was resonantly excited from the ground to the long-lived 12-4-keV excited state by 12.4-keV x-rays for the first time.
- The resonance energy that was known before the experiment to an uncertainty of  $\pm 50$  eV was determined with a sub-eV accuracy as  $12,389.59^{+0.15(\text{stat})}_{+0.12(\text{syst})}$  eV.
- High repetition-rate, narrow-band XFELs is an ideal platform to drive and study long-lived nuclear resonances at energies of hard X-rays. Development of XFELs is greatly desired.
- Successful resonant excitation of the  $^{45}\text{Sc}$  resonance opens up new horizons for ultra-high precision spectroscopy, extreme metrology in the regime of hard x-rays, and for a solid state  $^{45}\text{Sc}$  nuclear frequency standard (Mössbauer nuclear clock).
- This was the first step. The next steps (NFS etc.) will be as exciting but not easier. The first  $^{45}\text{Sc}$  NFS experiment is planned for October 2024 at EuXFEL.





# Summary and Outlook

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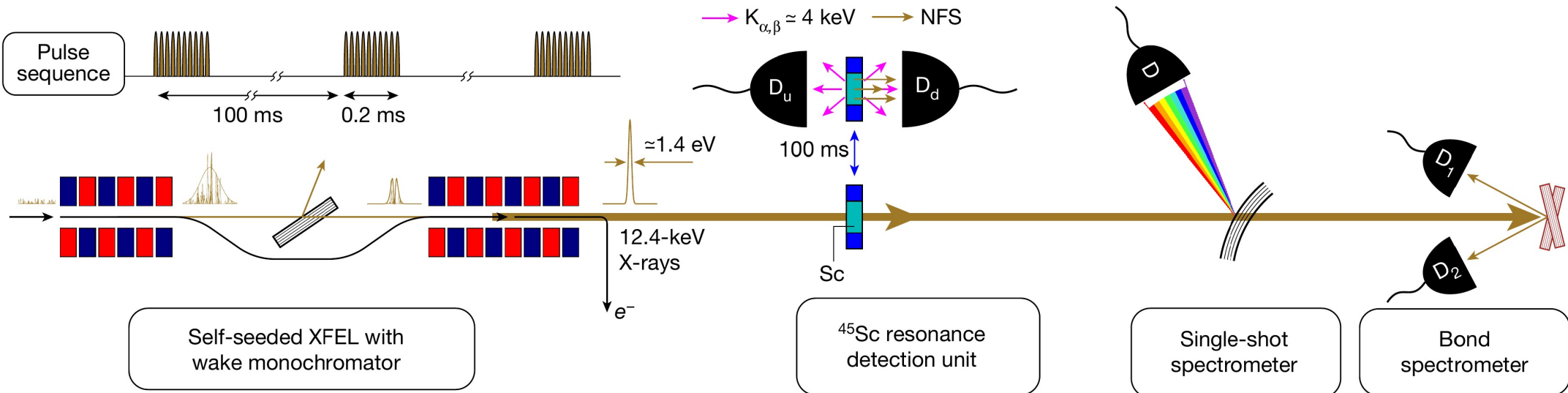
Thank you very much  
for your attention!

# Supplementary Slides

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# Experimental Setup and Experiment Execution



Eu XFEL provided for the experiment:

- $\Rightarrow$  0.2-ms pulse trains every 100 ms
- $\Rightarrow \approx 5 \times 10^{14}$  ph/s/eV  $\Rightarrow$  1.4 W
- $\Rightarrow \approx 0.7$  ph/s/ $\Gamma_0$
- $\Rightarrow$  tunable in a  $\pm 50$  eV range.

Target:  $\Rightarrow$  a 25- $\mu\text{m}$  Sc-metal foil;

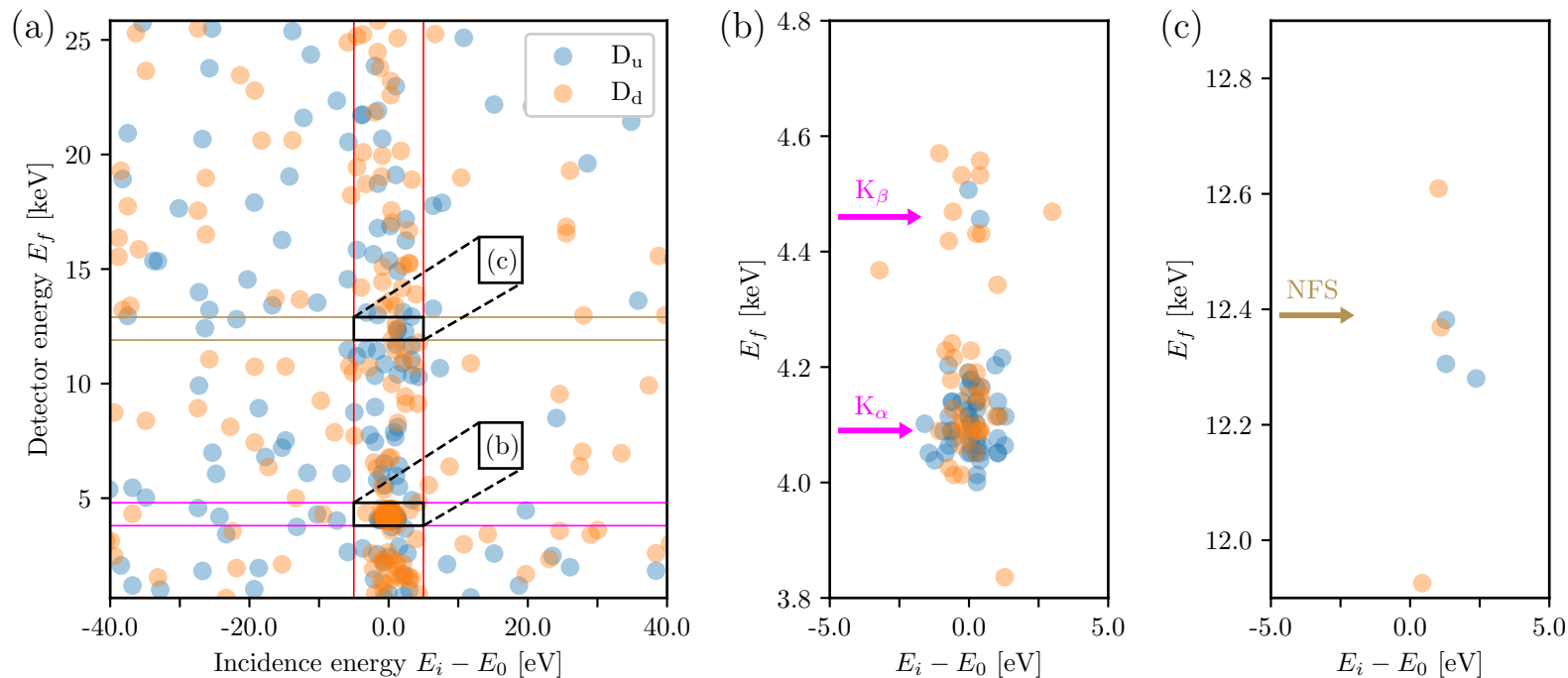
- $\Rightarrow$  moved between irradiation and detection locations every 100 ms (transient time  $< 20$  ms);
- $\Rightarrow$  water and air cooled.

$\Rightarrow$  Single-shot relative

- resolution and stability  $< 50$  meV;
- $\Rightarrow$  Bond spectrometer absolute resolution  $< 300$  meV.

Detectors  $D_1$ - $D_2$  had very low background  $< 2$  counts/10000 s since they  $\Rightarrow$  were inhibited during irradiation;  $\Rightarrow$  placed 12-mm off the 12.4-keV beam;  $\Rightarrow$  had  $< 150$ -eV energy resolution.

# Searching for $^{45}\text{Sc}$ Resonance



(a) Counts from the  $D_u$  and  $D_d$  x-ray detectors plotted as the energy  $E_f$  of the detected X-ray photons versus incident X-ray photon energy  $E_i - E_0$ . The photons were recorded in a time window of about 20-80 ms after every pulse-train excitation.

(b) Close-up of the 4.3-keV ROI, showing two clusters of counts centered at the energies of Sc  $K_\alpha$  (4.09 keV) and  $K_\beta$  (4.46 keV) fluorescence. This is a direct confirmation of detection of the  $^{45}\text{Sc}$  resonance.

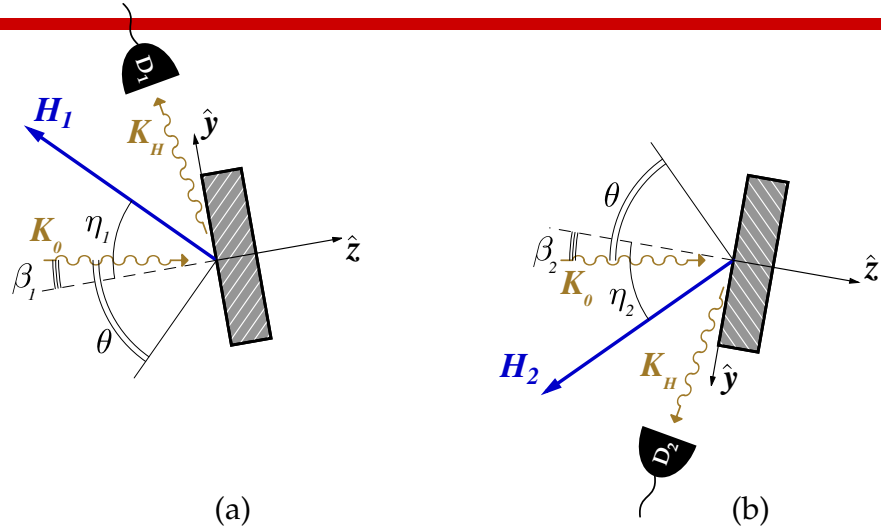
(c) Close-up of the 12.4-keV ROI. NFS signal at 12.4 keV is statistically insignificant. NFS is the prime next goal.

# Measurement of $^{45}\text{Sc}$ Nuclear Resonance Transition Energy

The  $^{45}\text{Sc}$  nuclear resonance transition energy  $E_0$  previously known to an uncertainty of  $\simeq \pm 50$  eV only, was determined with more than a hundred times higher accuracy as

$$E_0 = 12,389.59^{+0.15(\text{stat})}_{+0.12(\text{syst})} \text{ eV}$$

using Bond technique.



Bond technique uses Bragg diffraction of X-rays with wavevector  $K_0$  from atomic planes with diffraction vectors (a)  $H_1 = (8\ 0\ 0)$  and (b)  $H_2 = (0\ 8\ 0)$  from a Si crystal. The crystal is rotated by  $\beta = \beta_1 + \beta_2$  between the angular positions of the  $(8\ 0\ 0)$  and the  $(0\ 8\ 0)$  Bragg reflections. X-ray wavelength  $\lambda = 2\pi/K_0$  and photon energy  $E$  are calculated from the known crystal lattice parameter  $a_{\text{Si}}$  using modified Bragg's law:

$$\lambda = \frac{hc}{E} = \frac{a_{\text{Si}}}{4} \sin(\pi/4 + \beta/2). \quad (1)$$

W.L. Bond, Acta Crystallogr. 13 (1960) 814.

# $^{45}\text{Sc}$ Parameters

Parameters of  $^{45}\text{Sc}$ , taken from or based on Ref. [31] unless otherwise stated, with updated values measured or used in this work highlighted in colored boxes.

Parameter	Notation	Magnitude
<b>Ground state</b>		
Spin & parity	$I_g^\pi$	$7/2^-$
Magnetic moment	$\mu_g$	$+4.756487(2) \mu_N$
Quadrupole moment	$Q_g$	$-0.22(1) \text{ b}$
Isotopic abundance	$\eta$	100%
<b>Excited state</b>		
Energy	$E_0$	12,400(50) eV [31,48,49] 12,389.59 $^{\pm 0.15(\text{stat})}_{+0.12(\text{syst})}$ eV
Lifetime	$\tau_0$	470(6) ms [10,31,50]
Natural line width	$\Gamma_0 = \hbar/\tau_0$	1.40(2) feV
Quality factor	$Q = E_0/\Gamma_0$	$8.85(10) \times 10^{18}$
Multipolarity		M2
Spin & parity	$I_e^\pi$	$3/2^+$
Magnetic moment	$\mu_e$	$+0.368(5) \mu_N$ [51]
Quadrupole moment	$Q_e$	$+0.318(22) \text{ b}$ [51]
Internal conversion (IC) coefficients	$\alpha, \alpha_K$	632(71), 474 [31,50,52] 424, 363 [37]
Cross section	$\sigma_0$	$1.26(15) \times 10^{-20} \text{ cm}^2$ $1.9(5) \times 10^{-20} \text{ cm}^2$

[10] R.E. Holland, F.J. Lynch, K.E. Nystén, PRL 13 (1964) 241-243.

[31] Burrows, T. W., Nuclear Data Sheets 109, 171-296 (2008).

[37] Kibedi, T., et al., NIM A 589, 202-229 (2008).

[48] Freedman, M. S., et al., Phys. Rev. 140, B563-B565 (1965).

[49] Porter, F. T., et al., Phys. Rev. 146, 774-780 (1966).

[50] Blaugrund, A. E., et al., Phys. Rev. 159, 926-930 (1967).

[51] Gangrsky, Y. et al. Hyperfine Interact. 171, 209-215 (2006).

[52] Jones, K. W. and Schwarzschild, Phys. Rev. 148, 1148-1150 (1966).



# $^{57}\text{Fe}$ Nuclear Forward Scattering Demonstrated in 1991

VOLUME 66, NUMBER 6

PHYSICAL REVIEW LETTERS

11 FEBRUARY 1991

## Mössbauer Spectroscopy Using Synchrotron Radiation

J. B. Hastings, D. P. Siddons, U. van Bürc, <sup>(a)</sup> R. Hollatz, <sup>(b)</sup> and U. Bergmann <sup>(c)</sup>

<sup>(a)</sup>National Synchrotron Light Source, Brookhaven National Laboratory, Upton, New York 11973  
<sup>(b)</sup>(Received 12 October 1990)

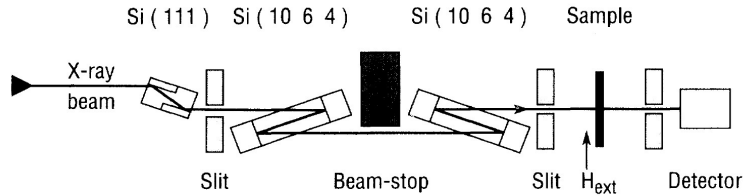
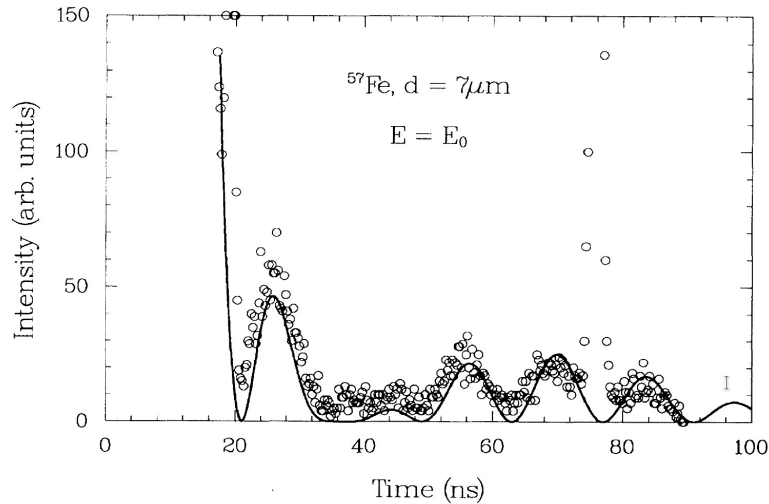


FIG. 1. A schematic of the experimental configuration used.



JETP Lett., Vol. 53, No. 2, 25 Jan. 1991

Shvyd'ko *et al.*

## Observation of intensified forward $\gamma$ -ray emission in spontaneous nuclear decay

Yu. V. Shvyd'ko, G. V. Smirnov, and S. L. Popov T. Hertrich

<sup>(a)</sup>I. V. Kurchatov Institute of Atomic Energy, 123182, Moscow <sup>(b)</sup>Technical University Munich, Garching D-8048, FRG

(Submitted 29 November 1990)

Pis'ma Zh. Eksp. Teor. Fiz. 53, No. 2, 69-73 (25 January 1991)

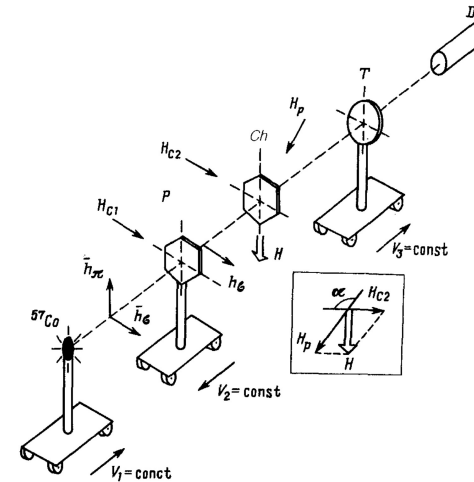


FIG. 1. Experimental layout. 14.4-keV source of Mössbauer  $\gamma$  rays [ $^{57}\text{Co}(\text{Cr})$ ]; ( $^{57}\text{FeBO}_3$ ); radiation chopper  $Ch$  ( $^{57}\text{FeBO}_3$ ); nuclear-resonance target  $T$  [ $\text{K}_2\text{MgF}_4$ ]; detector  $D$  (NaI).

